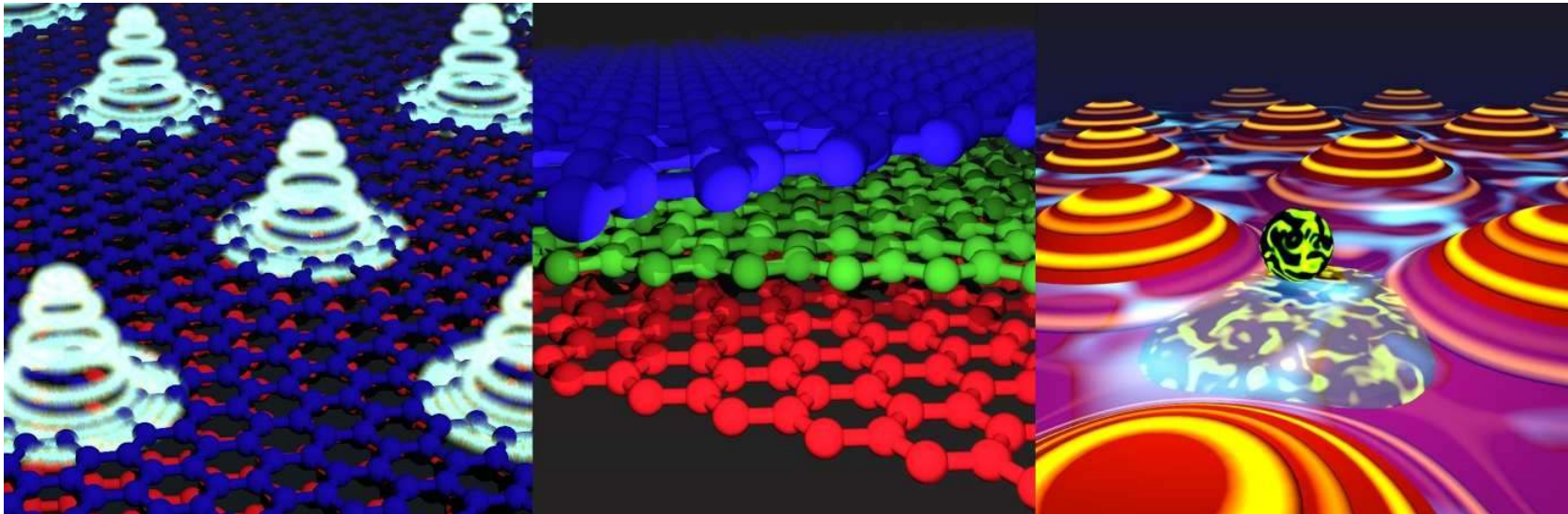


Atomic defects in topological and correlated twisted van der Waals heterostructures

Jose Lado

Department of Applied Physics, Aalto University, Finland



Phys. Rev. B 99, 245118 (2019)
Phys. Rev. Materials 3, 084003 (2019)

Phys. Rev. Research 2, 033357 (2020)

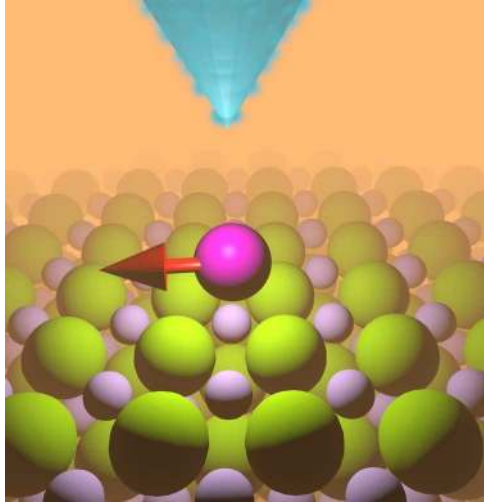
arXiv:2202.11003 (2022)

First-principles modeling of defects in solids, ETH Zürich, Switzerland

June 15th 2022

Building quantum matter with artificial lattices

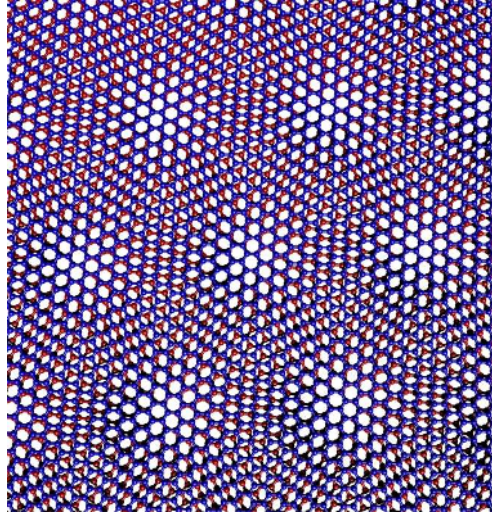
Atomic lattices



$a = 0.5 \text{ nm}$

Nature Physics 12 (7), 656 (2016)
Nature Physics 13 (7) 668 (2017)
Science 335 (6065), 196-199 (2012)

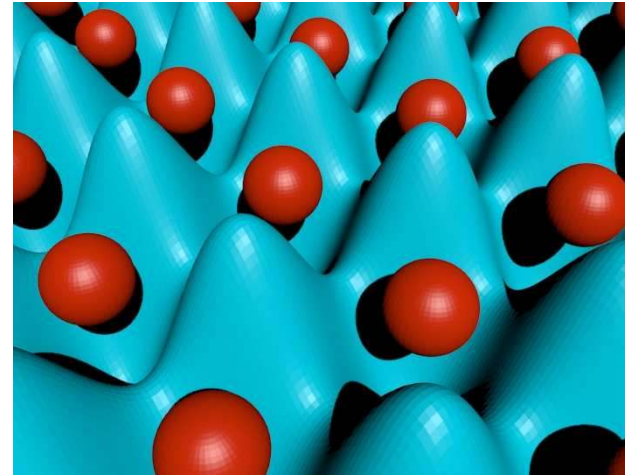
Twisted 2D moire materials



$a = 30 \text{ nm}$

Phys. Rev. Lett. 99, 256802 (2007)
Nature Physics 6, 109–113 (2010)
PNAS 108 (30) 12233-12237 (2011)
Nature 556, 80–84 (2018)

Cold atoms



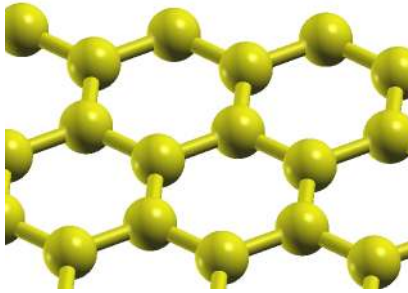
$a = 1000 \text{ nm}$

Nature 545, 462–466 (2017)
Nature 455, 204–207 (2008)
Phys. Rev. Lett. 111, 185307 (2013)

The two-dimensional materials world

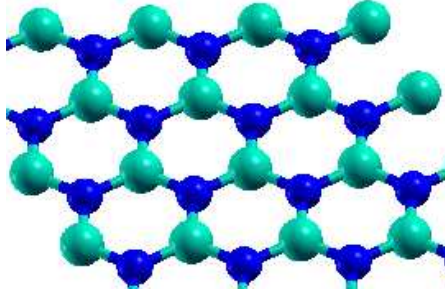
Semimetal

Graphene



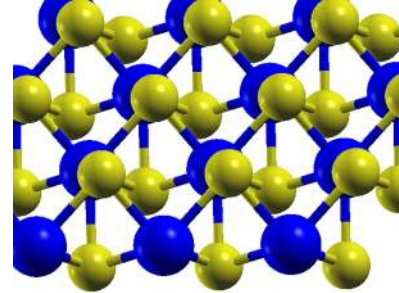
Insulator

BN



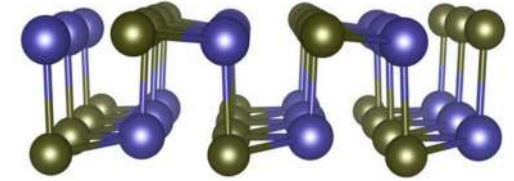
Superconductor

NbSe₂



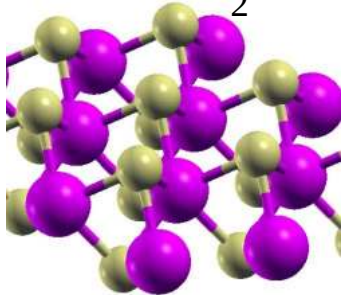
Ferroelectric

SnTe



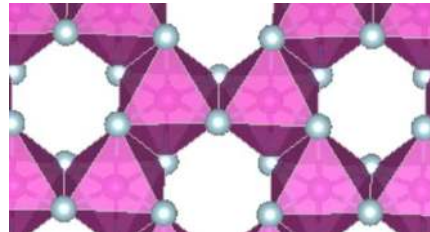
Semiconductor

WSe₂



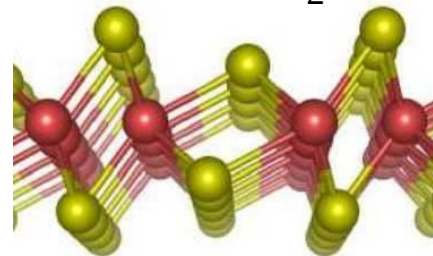
Ferromagnet

CrI₃



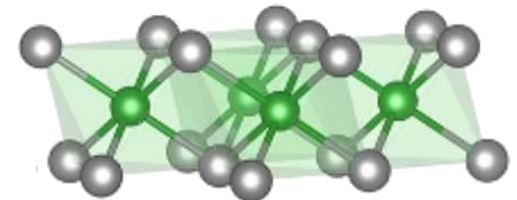
**Quantum spin
Hall insulator**

WTe₂



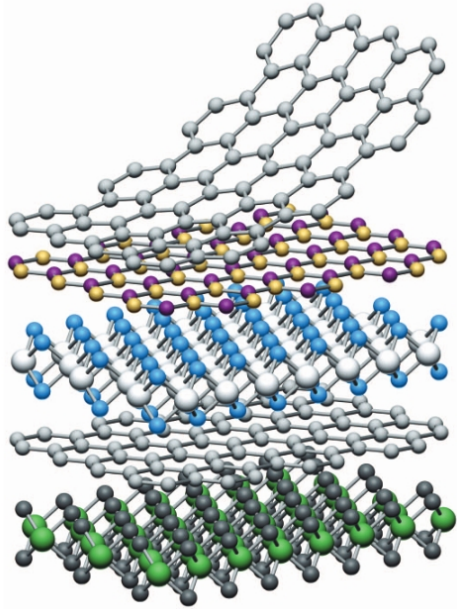
Multiferroic

NiI₂



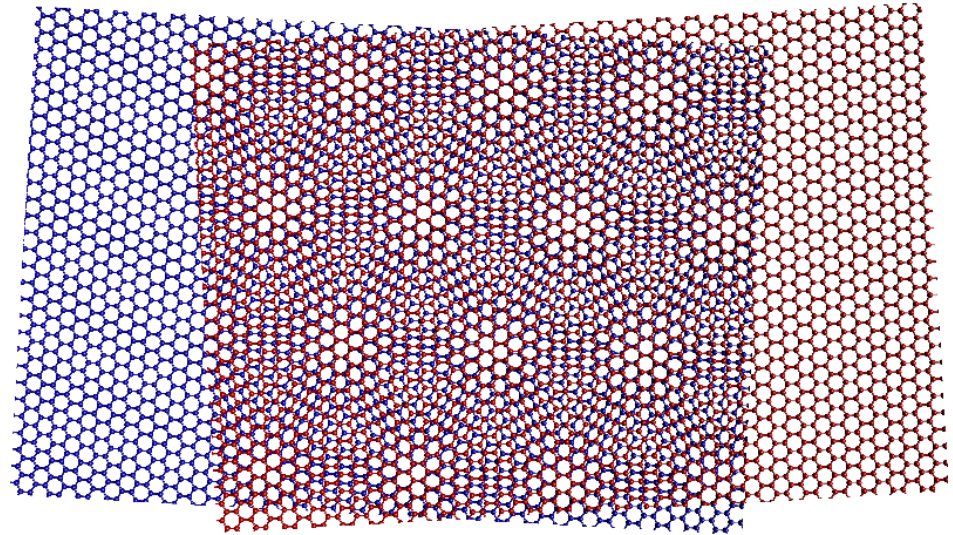
The flexibility of two-dimensional materials

They can be stacked



Nature 499.7459 419. (2013)

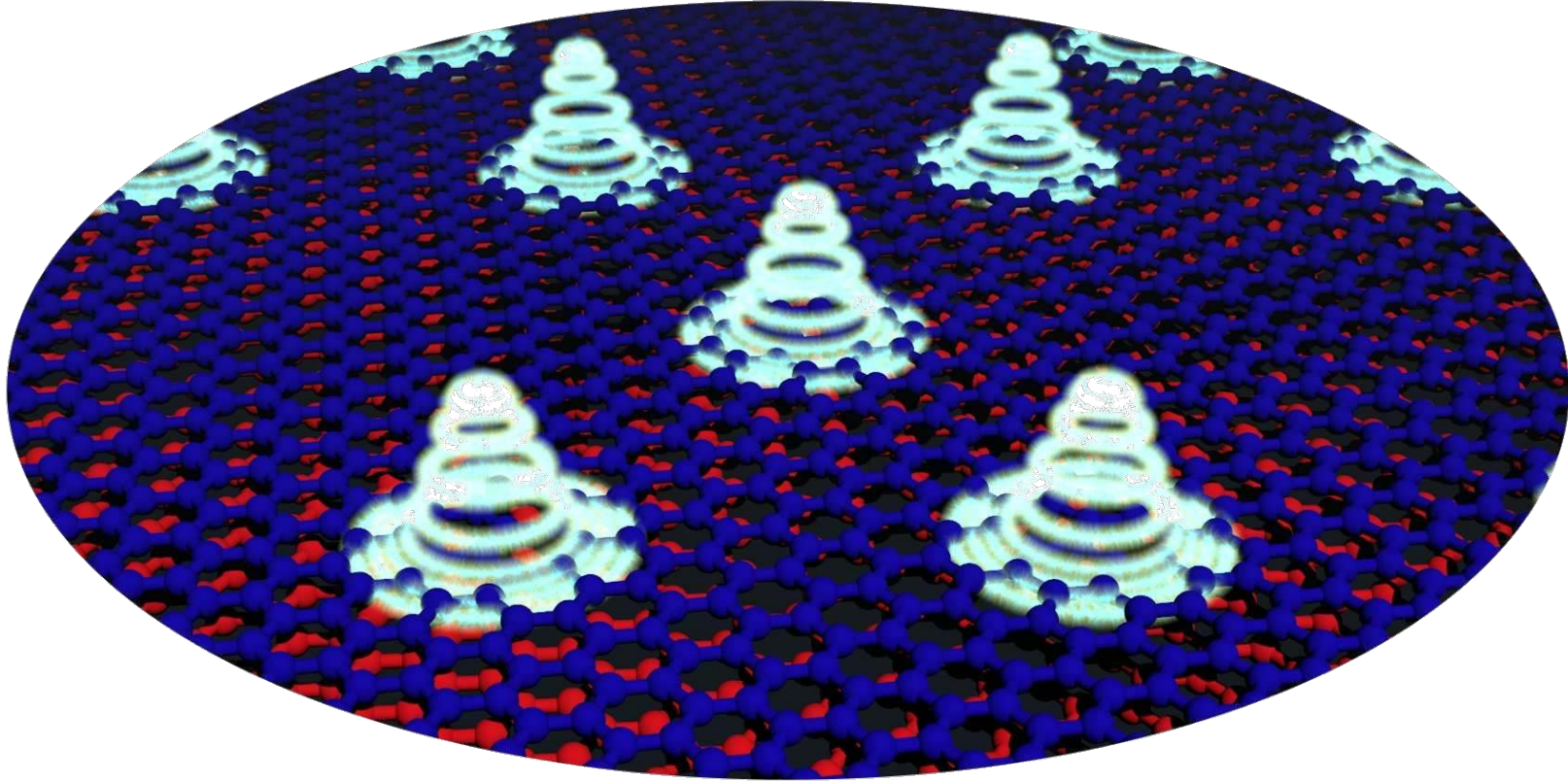
They can be rotated



Science 361.6403 690-693. (2018)

These are unique features of two-dimensional materials

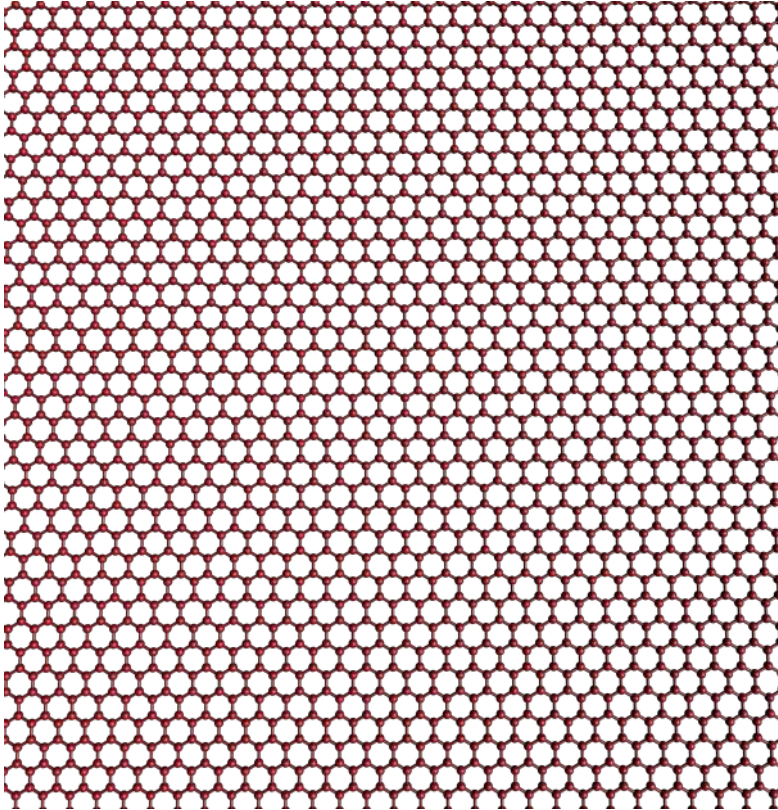
A new universe in each new twisted material



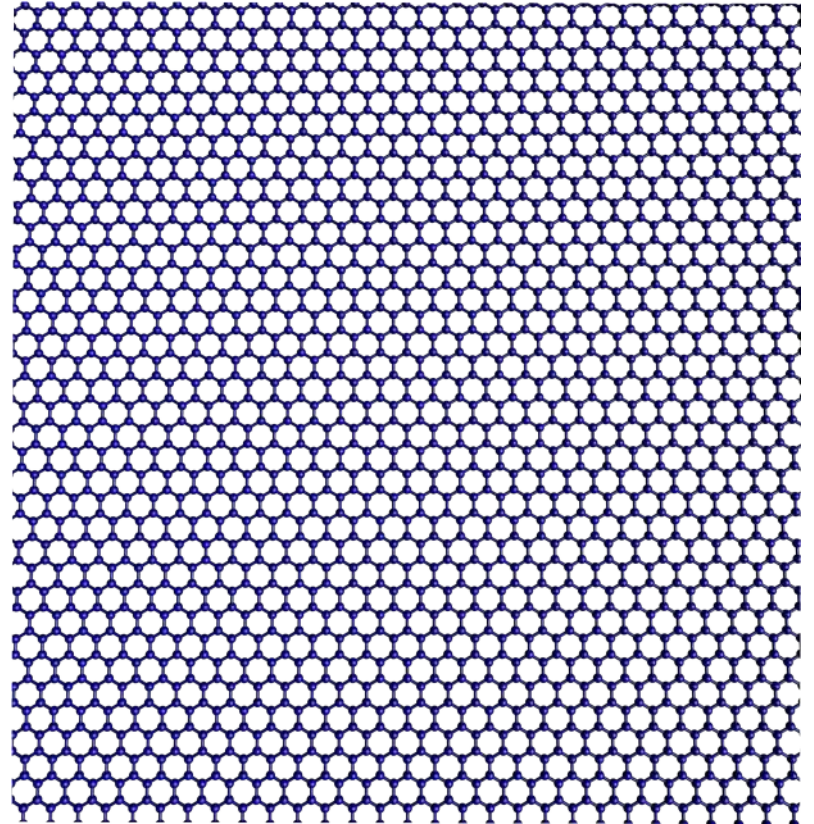
Each twisted material is a new universe for electrons, with laws that change from twist to twist

Moire in twisted bilayer graphene

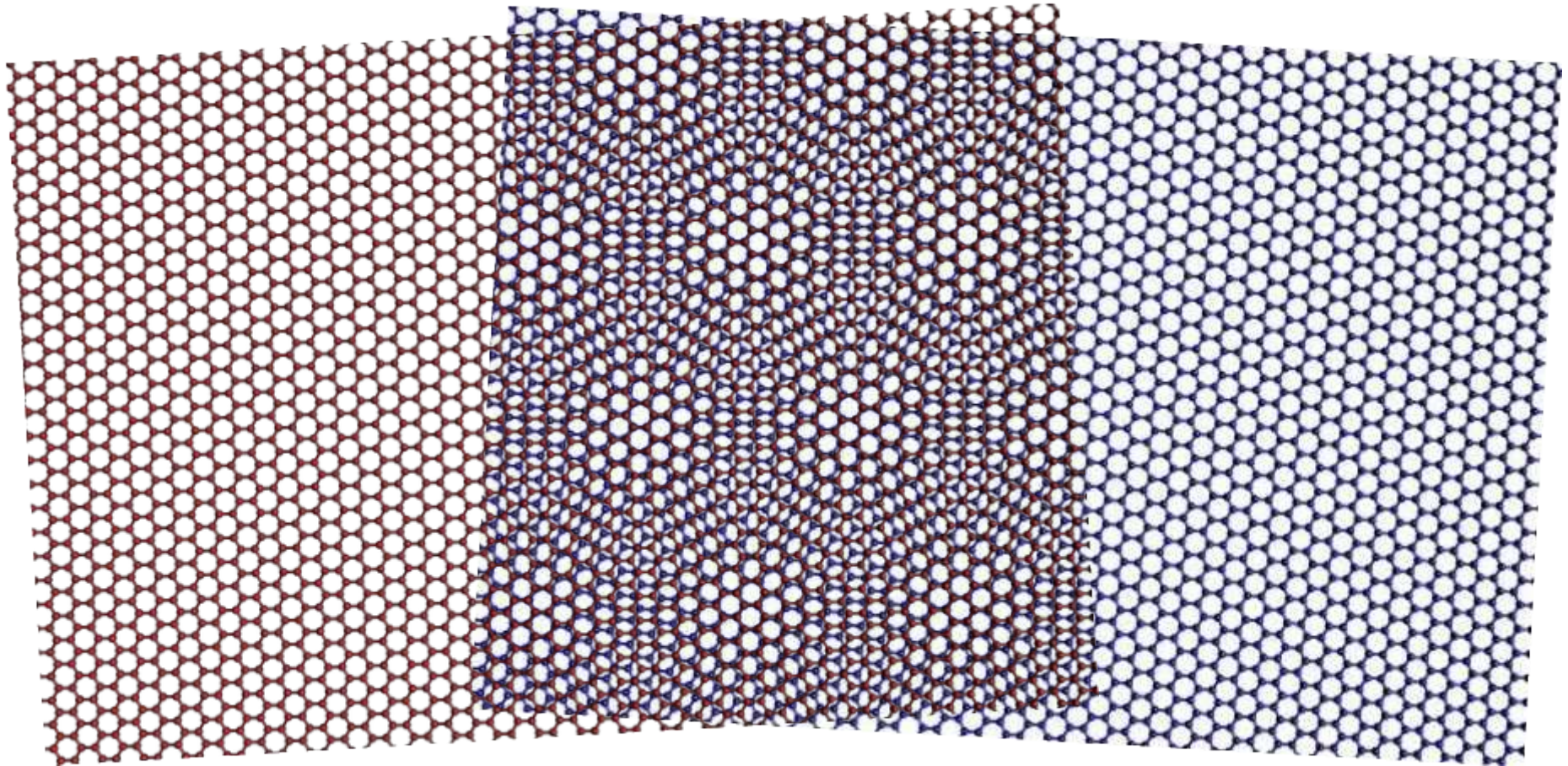
Upper graphene layer



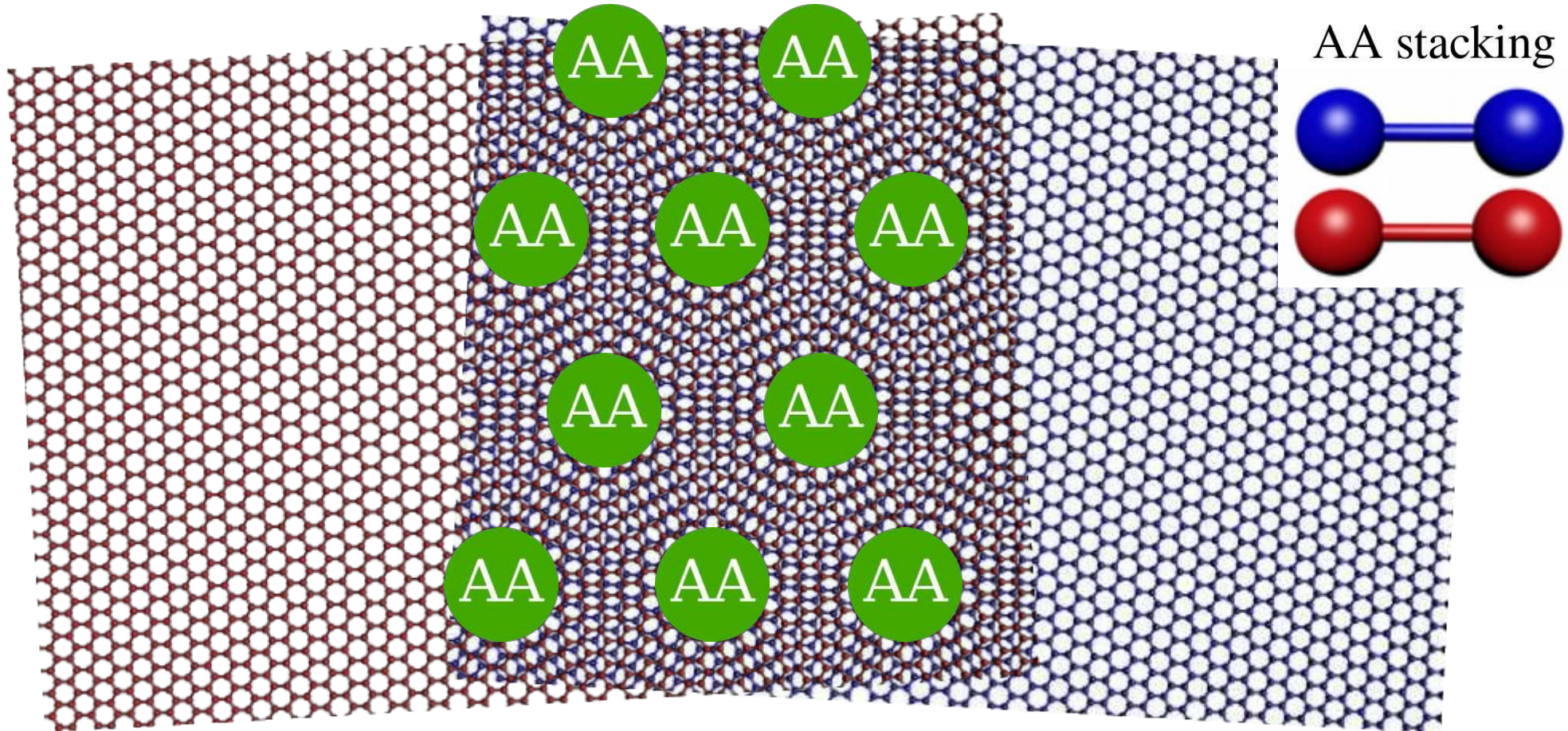
Lower graphene layer



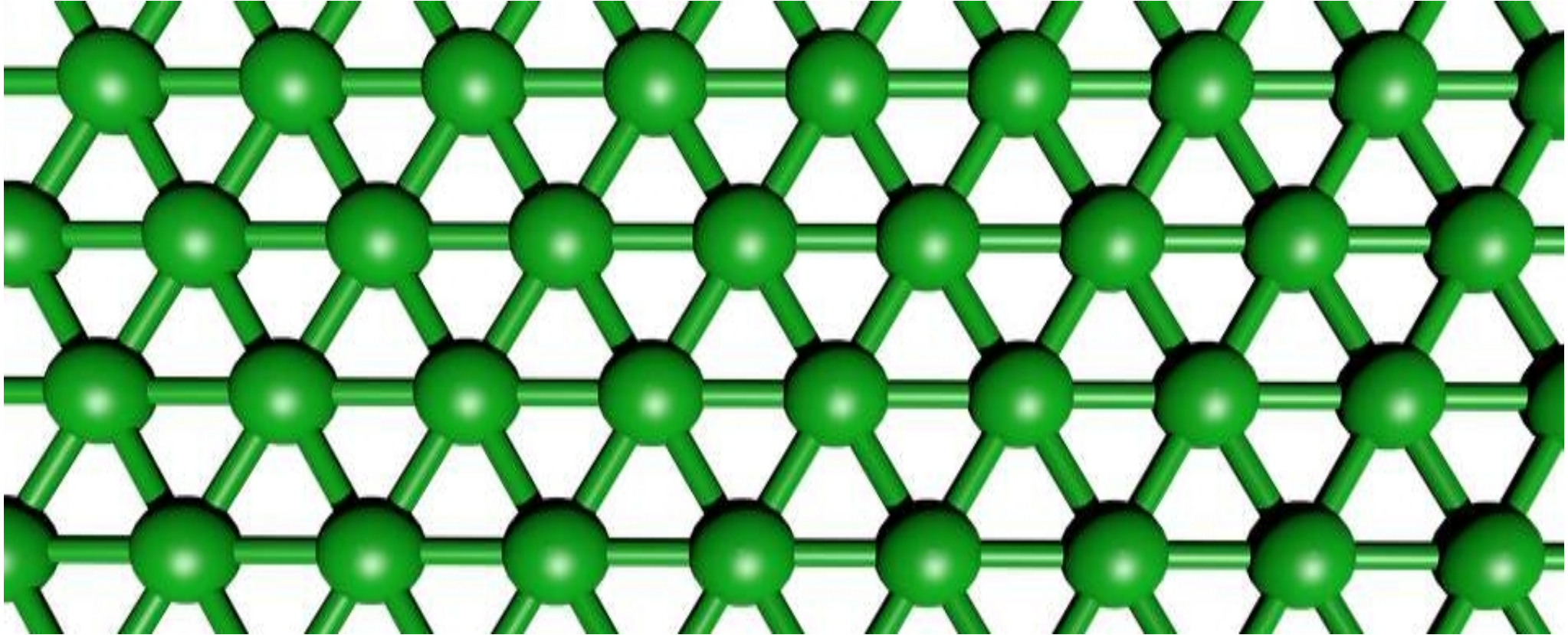
Moire in twisted bilayer graphene



Moire in twisted bilayer graphene

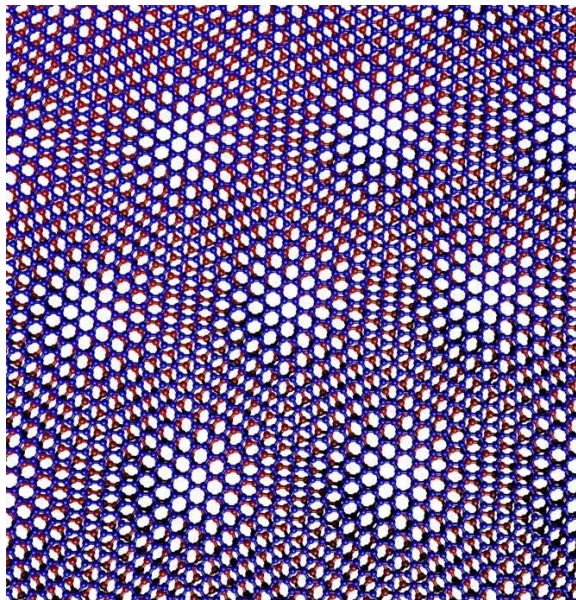


Moire in twisted bilayer graphene

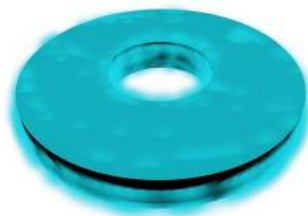


One material, a zoo of electronic phases

Twisted bilayer graphene

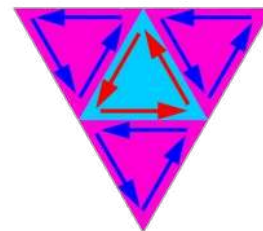


Superconductivity



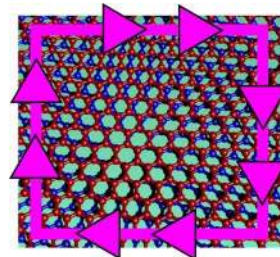
Nature 556, 43–50 (2018)

Topological networks



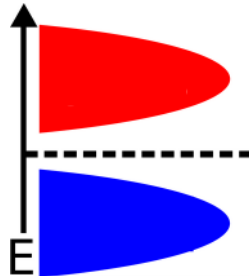
Nano Lett. 18, 11,
6725-6730 (2018)

Chern insulators



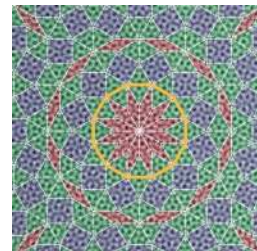
Science 365, 605-608 (2019)

Correlated insulators



Nature 556, 80–84 (2018)

Quasicrystalline physics



Science 361, 782-786 (2018)

Fractional Chern insulators



Nature 600, 439–443 (2021)

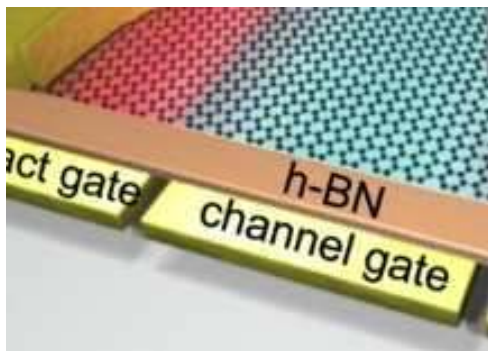
Twisted graphene multilayers provide a powerful platform for emergent phenomena

Controlling electronic states in twisted van der Waals materials

*Of course, we can use the typical knobs of bulk compounds
(pressure, chemical doping, etc)*

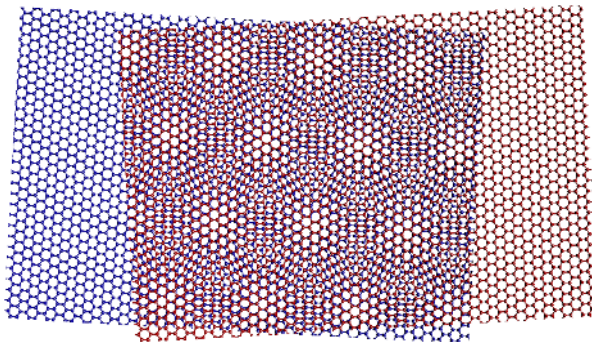
Most importantly, we can exploit the full tunability of van der Waals materials

Gating



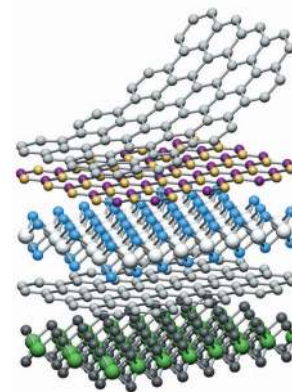
Science 306, 5696, 666-669 (2004)

Twist engineering



Nature Reviews Materials 6, 201–206 (2021)

Materials engineering



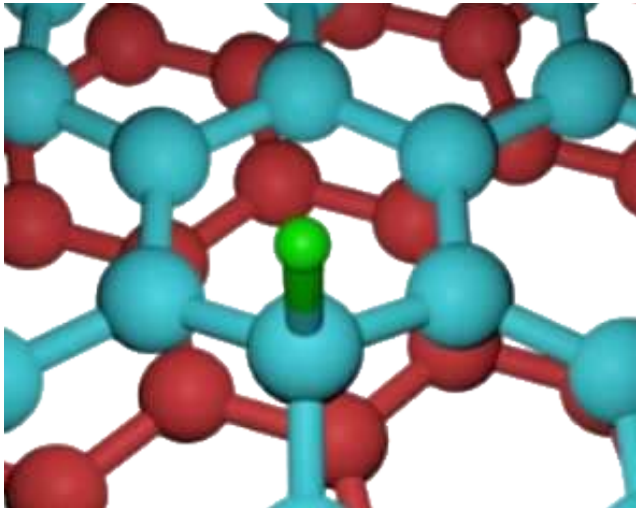
Nature 499, 419–425 (2013)

Allowing to independently control different features of the electronic structure

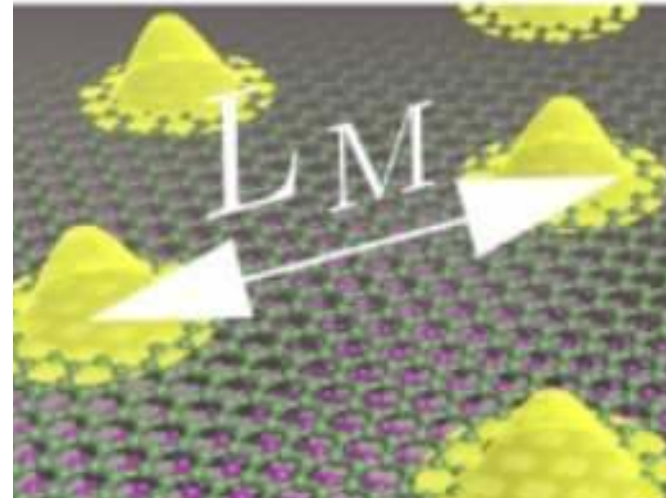
Defects in twisted van der Waals materials

Two length scales in moire systems

The original atomic scale



The emergent moire scale

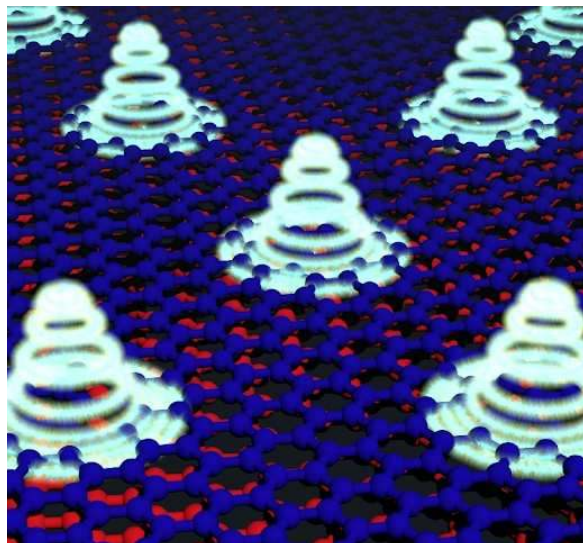


The coexistence of these two different scales is unique to moire systems

How do atomic impurities impact the physics emerging from much bigger length scales?

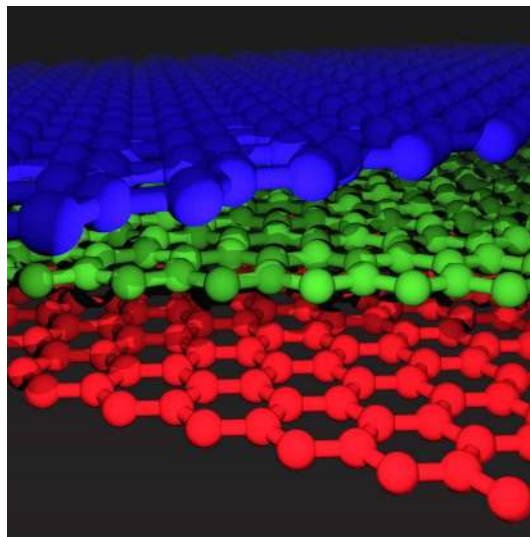
Today's plan

Impurities in twisted graphene bilayers



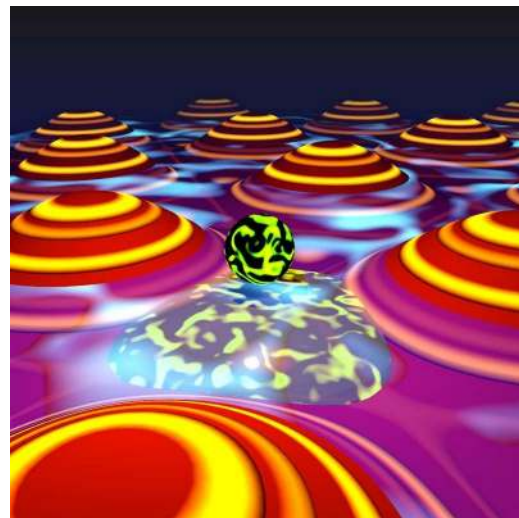
Phys. Rev. B 99, 245118 (2019)
Phys. Rev. Materials 3, 084003 (2019)

Impurities in twisted graphene trilayers



Phys. Rev. Research 2, 033357 (2020)

Impurities in twisted moire topological superconductors



arXiv:2202.11003 (2022)

Behind the scenes

*Impurities in twisted
graphene bilayers*



Aline Ramires

Phys. Rev. B 99, 245118 (2019)

*Impurities in twisted
graphene trilayers*



Alejandro Lopez Bezanilla

Phys. Rev. Research 2, 033357 (2020)
Phys. Rev. Materials 3, 084003 (2019)

*Impurities in twisted
moire topological superconductors*



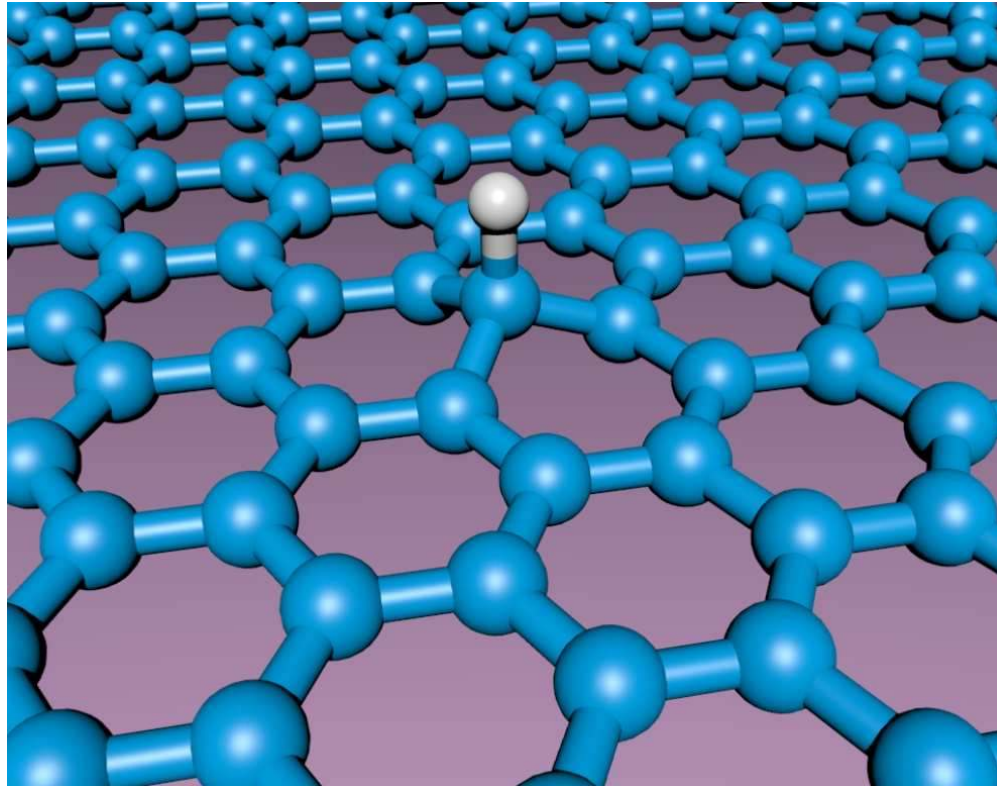
Maryam Khosravian

arXiv:2202.11003 (2022)

Impurities in twisted bilayer graphene

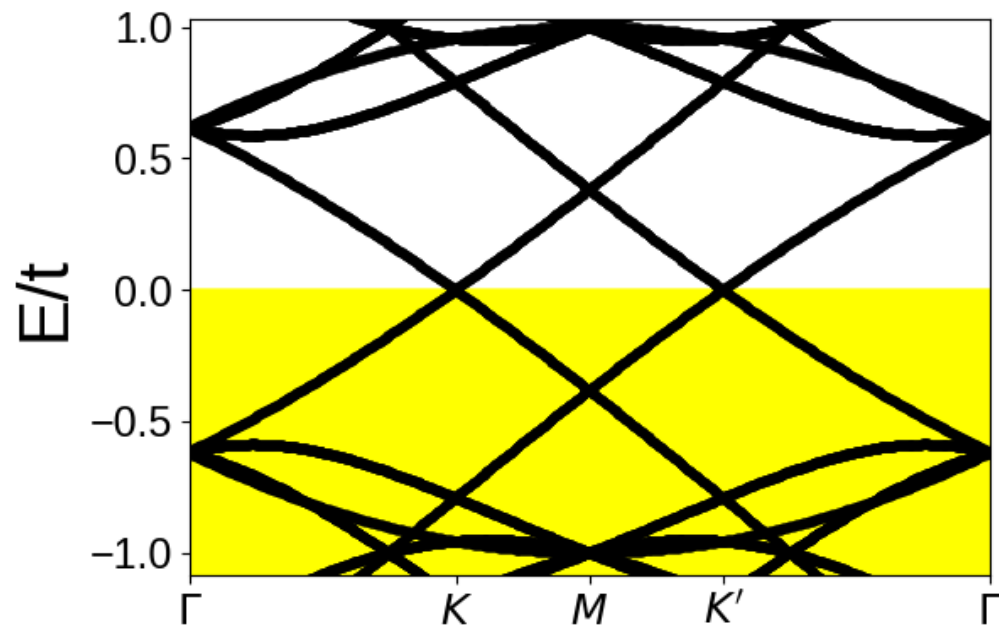
Impurities in monolayer graphene

Hydrogen adsorption in graphene

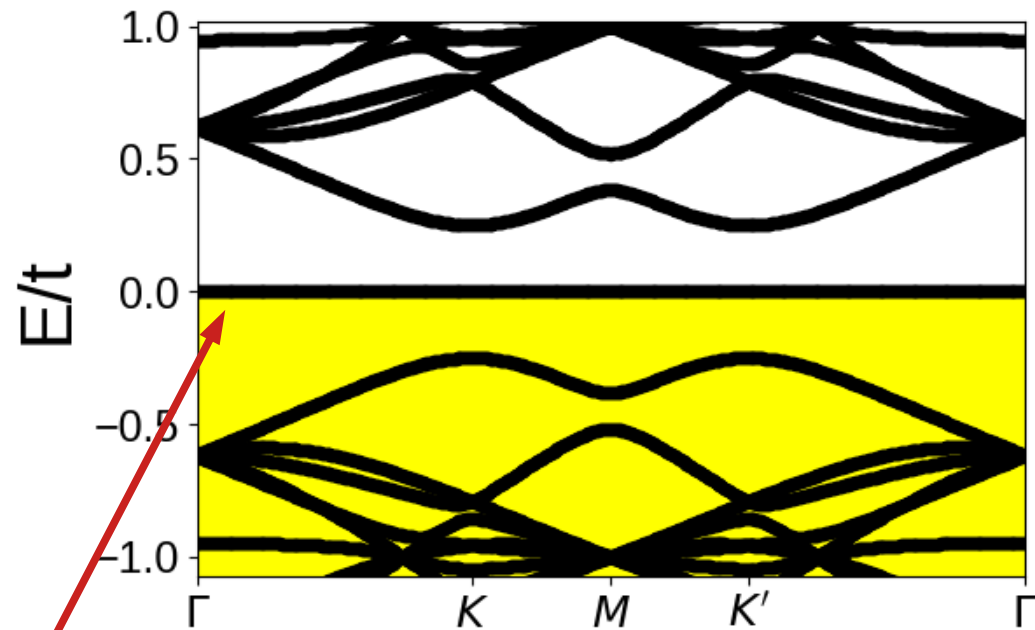


Impurities in monolayer graphene

Pristine 5x5 graphene supercell



Defect in a 5x5 graphene supercell

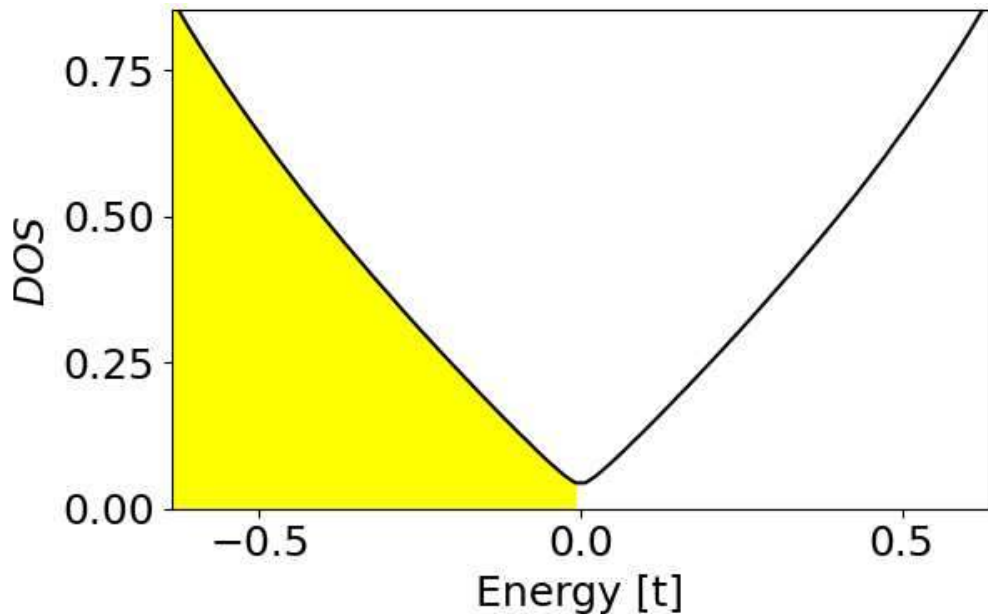


Phys. Rev. B 75, 125408 (2008)
Rep. Prog. Phys. 73 056501 (2010)

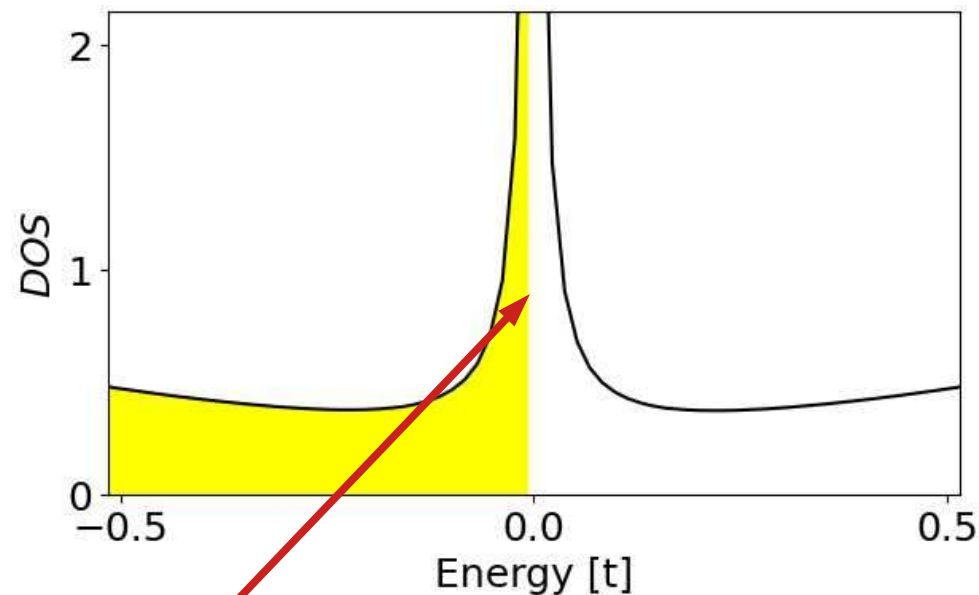
Hydrogen atoms create zero modes in graphene

Single impurity in monolayer graphene

Pristine graphene



Single impurity in infinite graphene

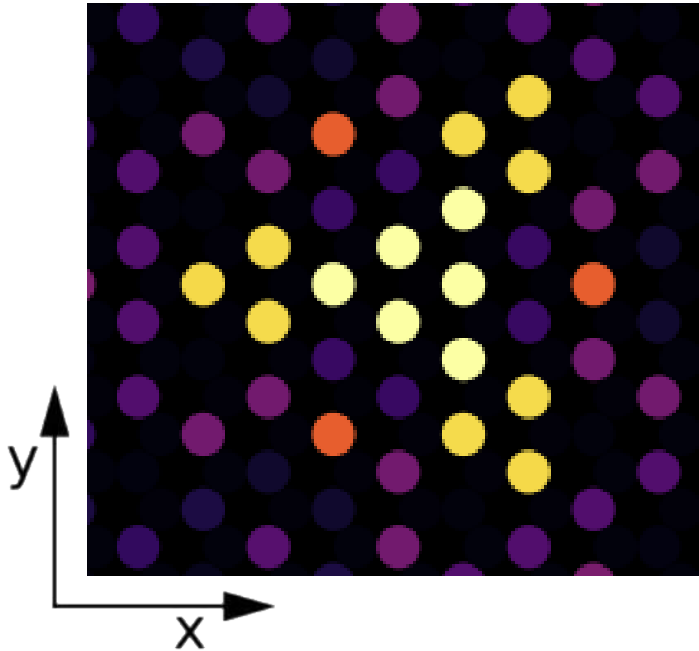


Phys. Rev. B 75, 125408 (2008)
Rep. Prog. Phys. 73 056501 (2010)

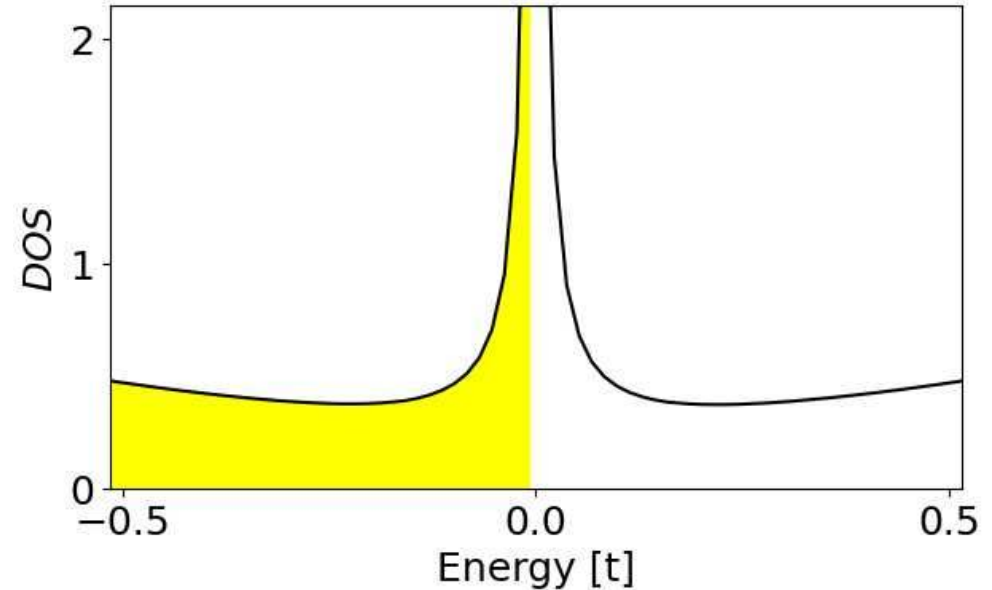
Hydrogen atoms create zero modes in graphene

Single impurity in monolayer graphene

Local density of states



Single impurity in infinite graphene

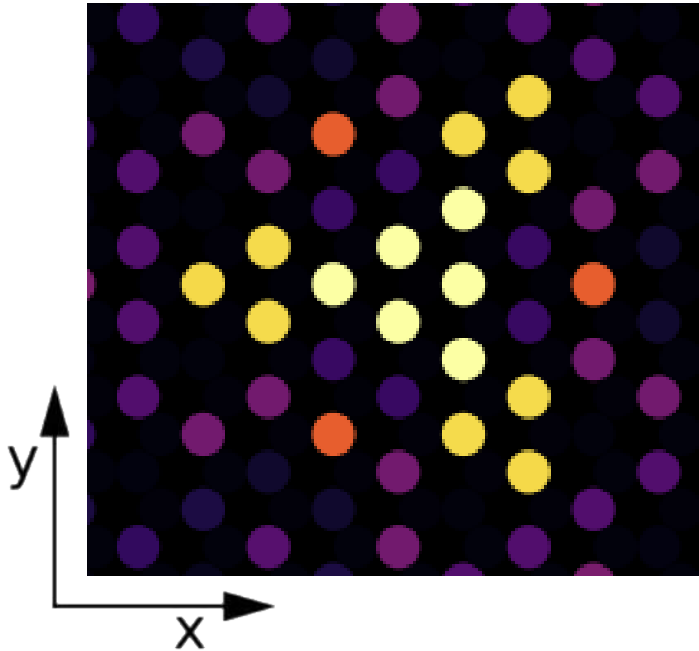


Phys. Rev. B 75, 125408 (2008)
Rep. Prog. Phys. 73 056501 (2010)

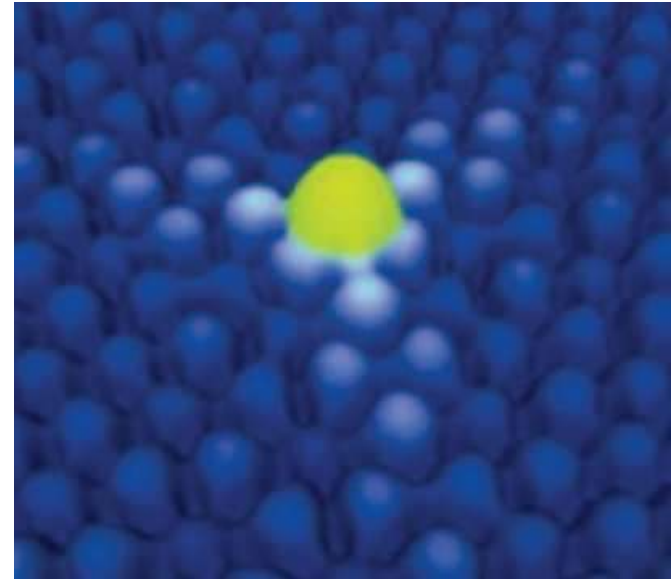
Hydrogen atoms create zero modes in graphene

Single impurity in monolayer graphene

Local density of states



Experimental local density of states

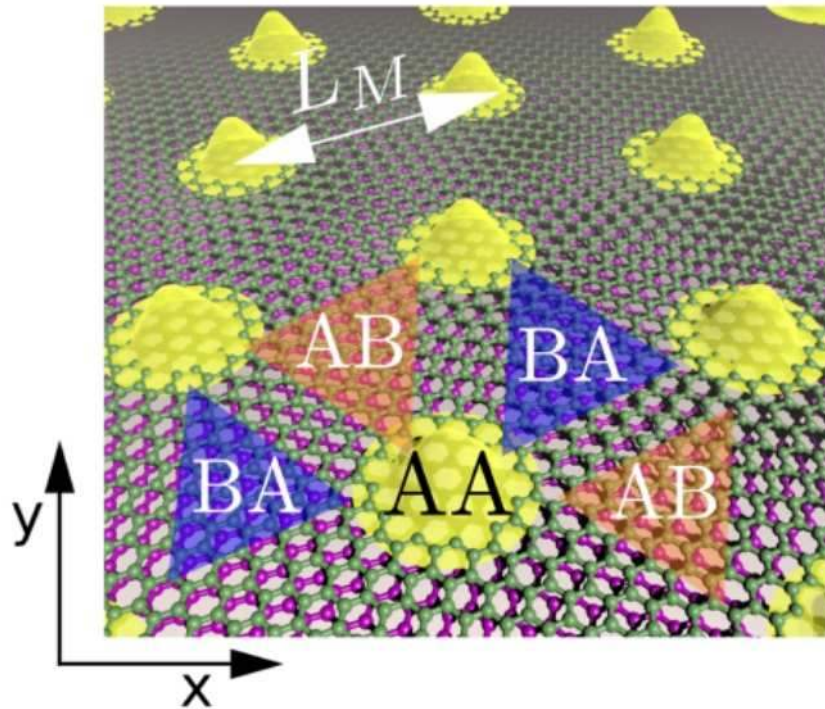


Science, 352(6284), 437-441 (2016)

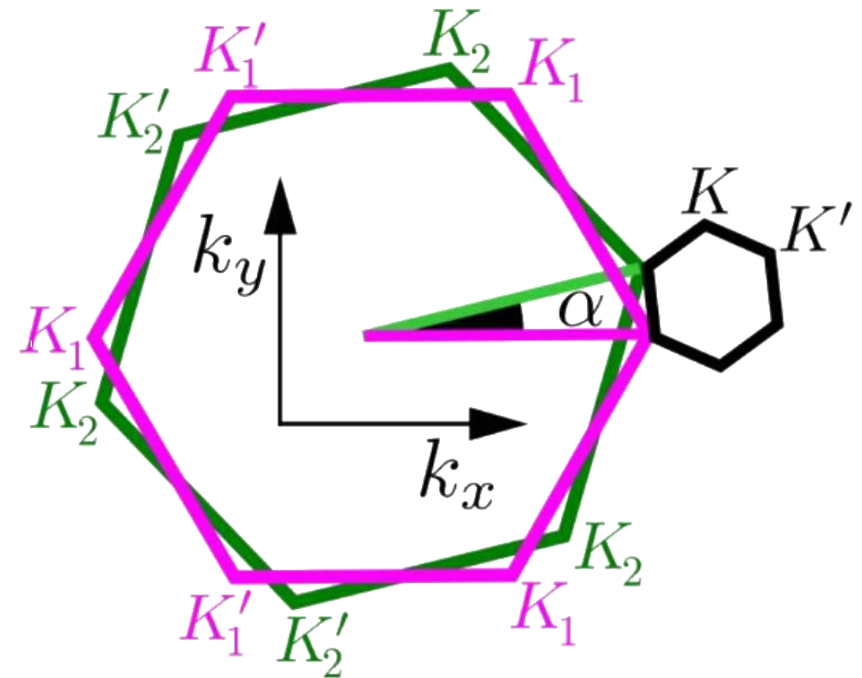
Hydrogen atoms create zero modes in graphene

Twisted graphene bilayers

Structure



Reciprocal space



Uncoupled layers

Dirac cone from layer #1

Momentum

Dirac cone from layer #2

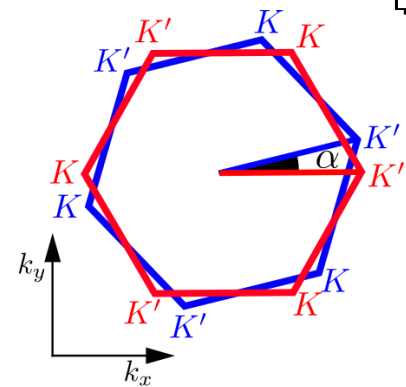
Energy

$$\Delta K \propto \alpha$$

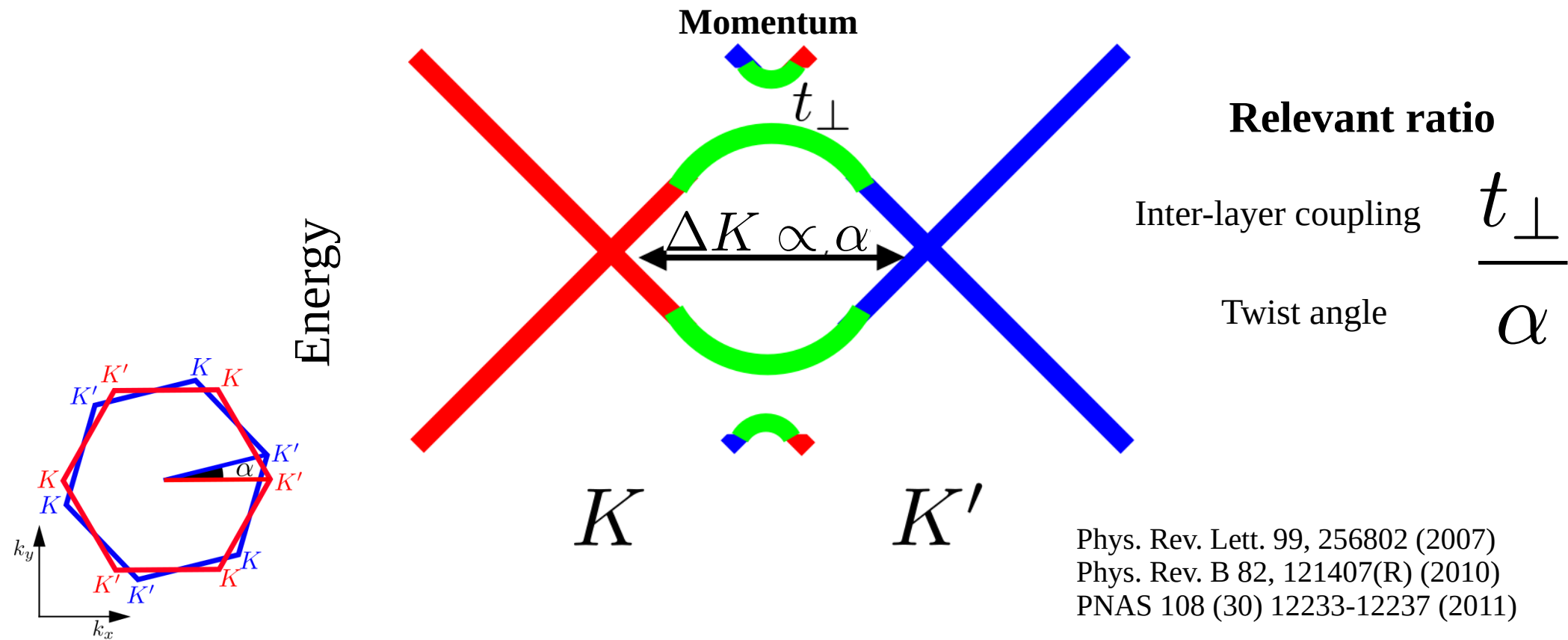
K

K'

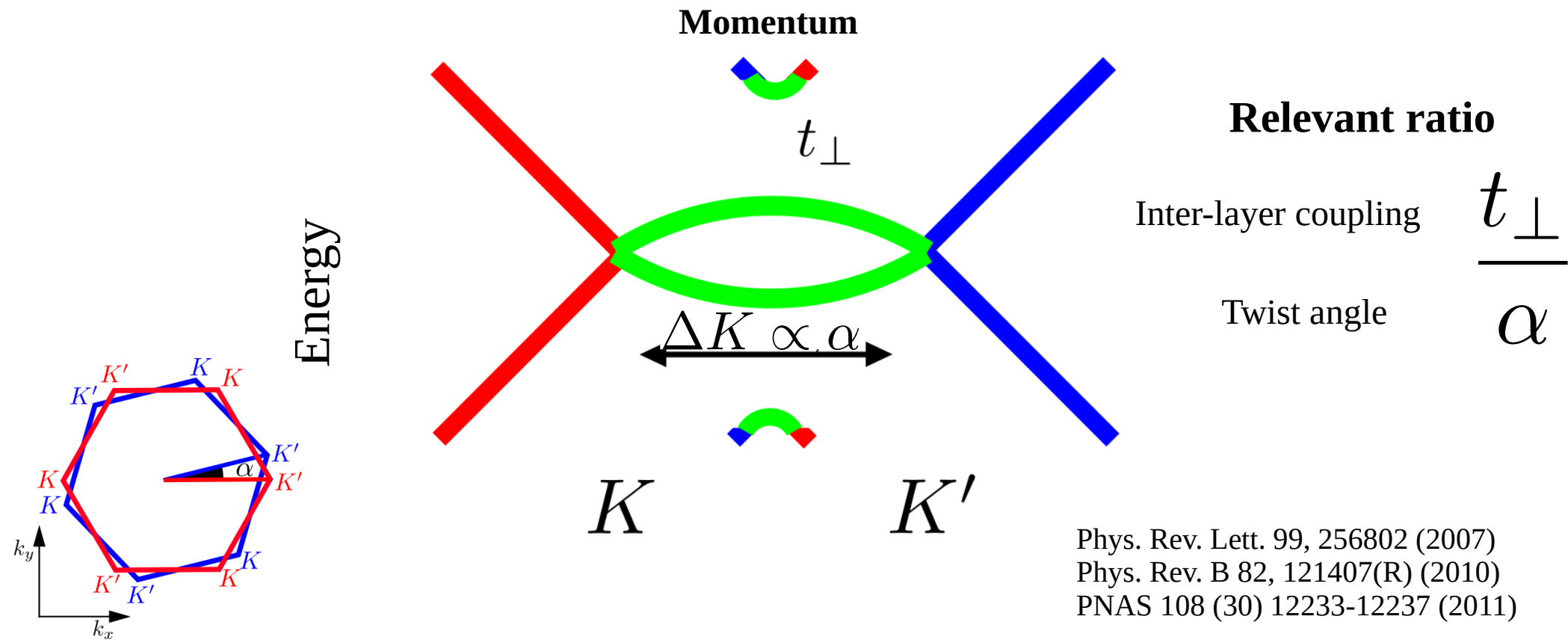
Phys. Rev. Lett. 99, 256802 (2007)
Phys. Rev. B 82, 121407(R) (2010)
PNAS 108 (30) 12233-12237 (2011)



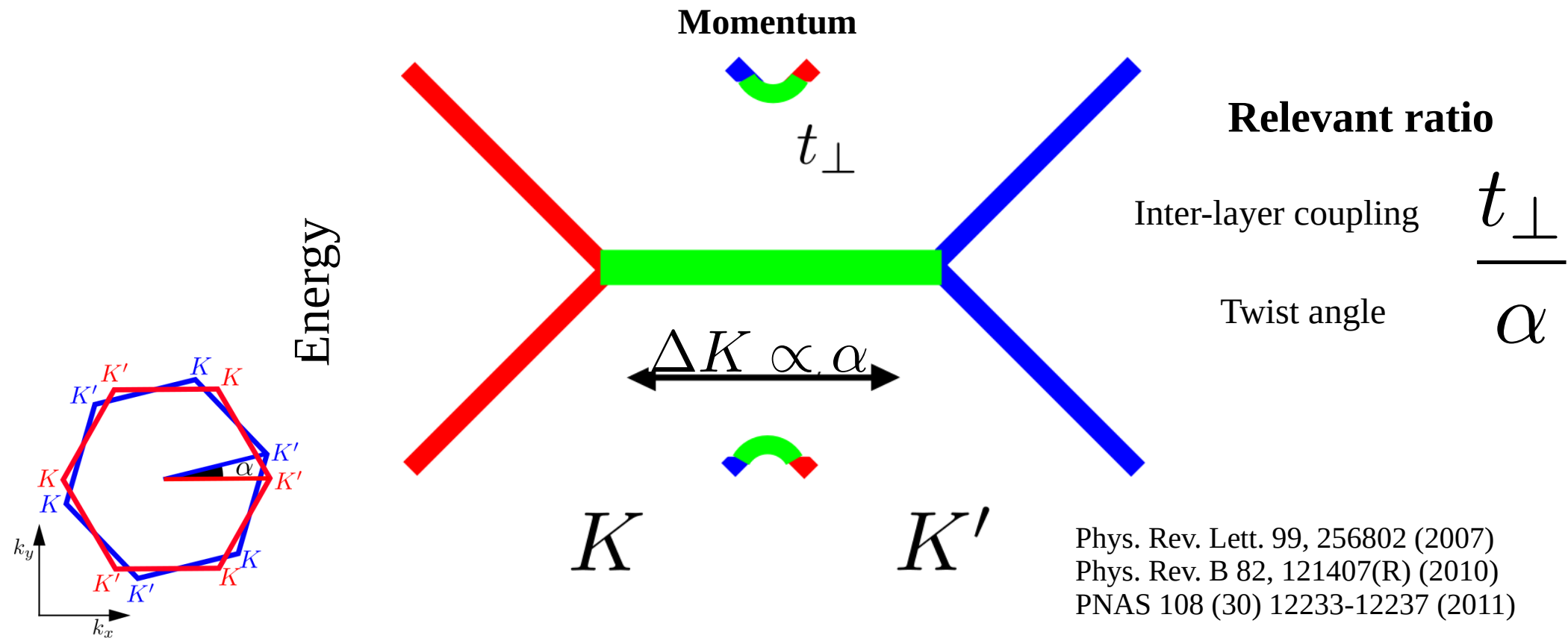
Coupling the layers



Coupling the layers

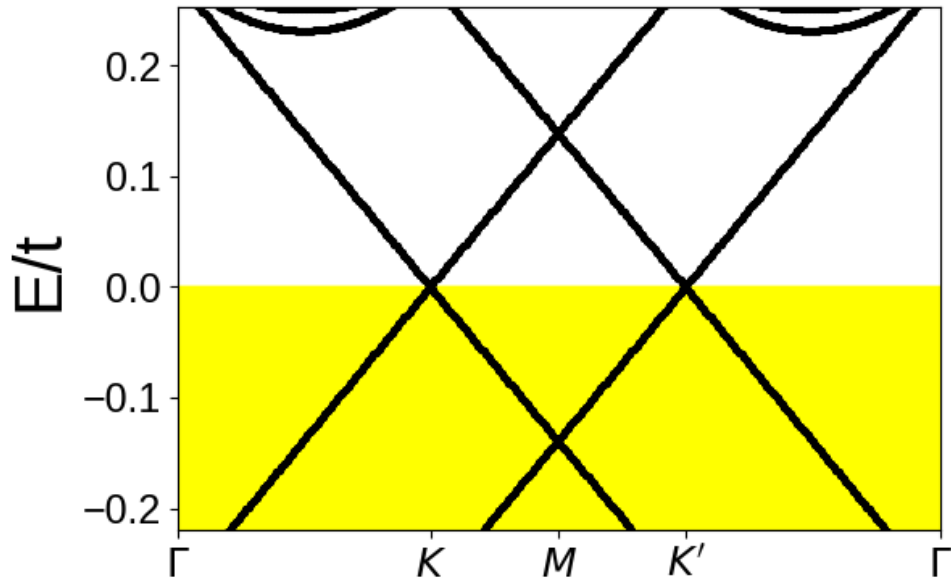


Coupling the layers

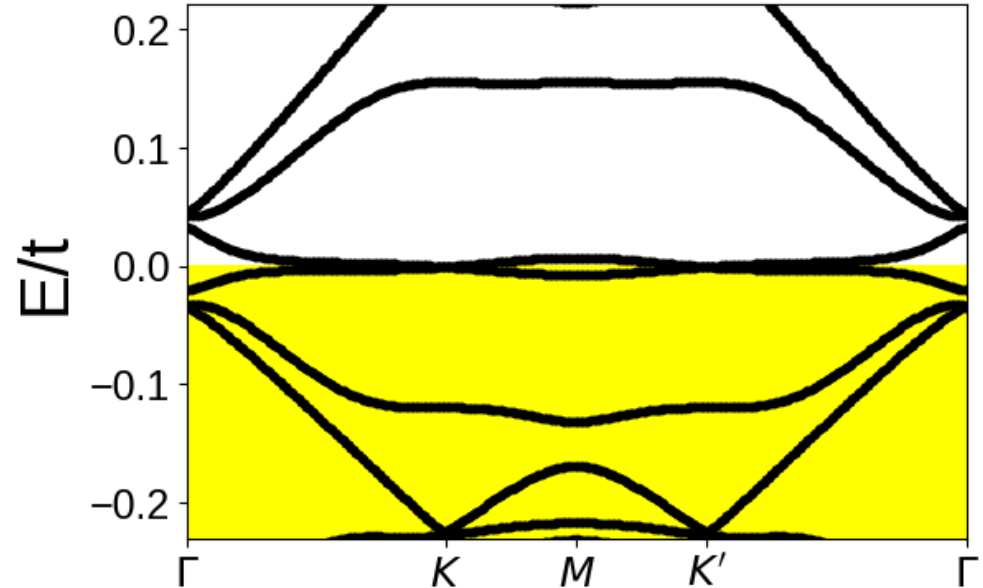


Electronic structure of twisted bilayer

Uncoupled layers



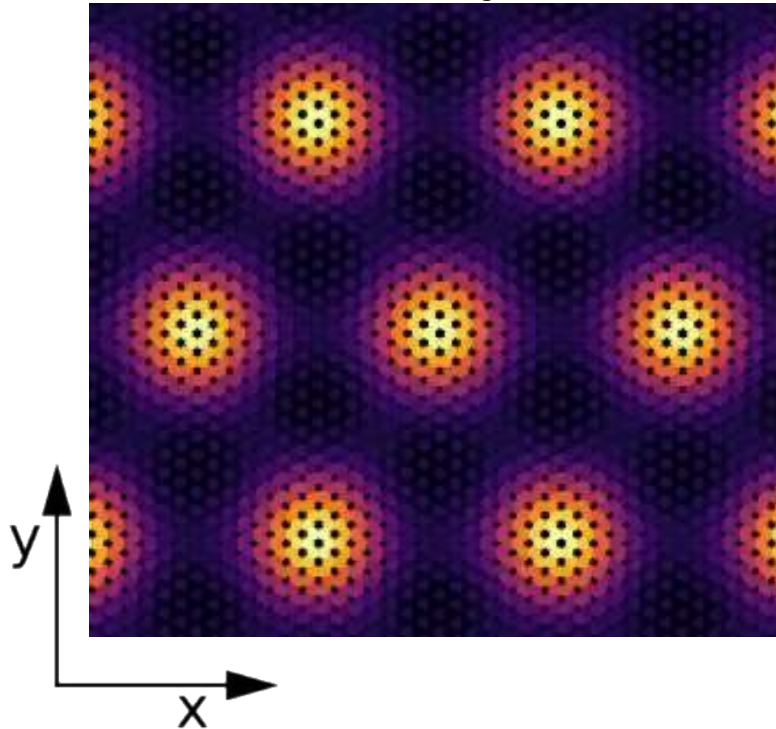
Coupled layers



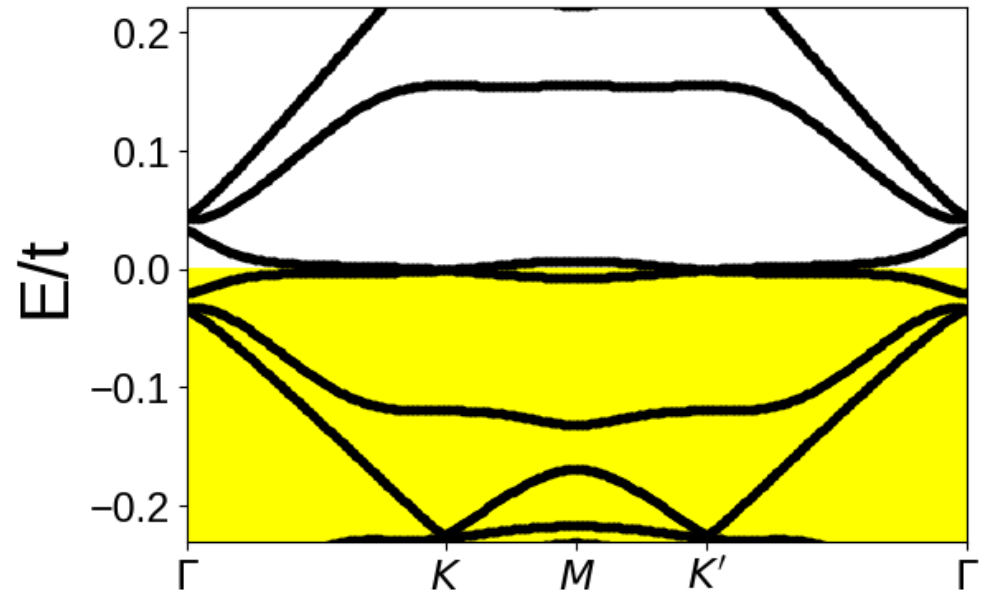
Twisted graphene bilayers feature flat bands driven by the twist

Electronic structure of twisted bilayer

Local density of states



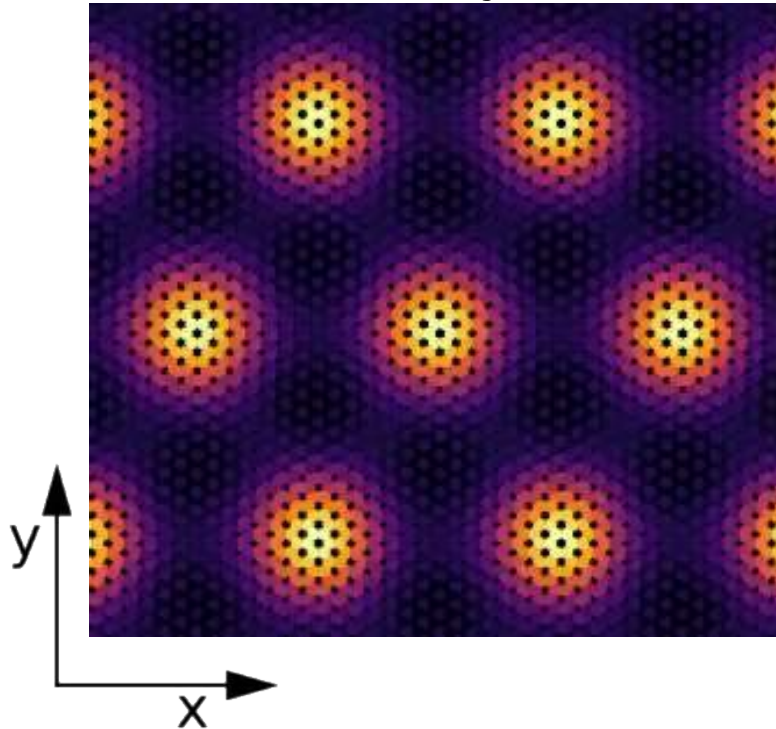
Coupled layers



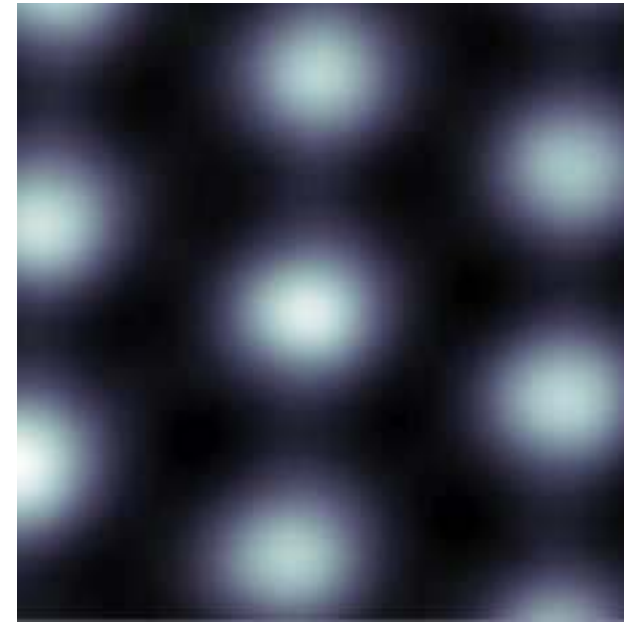
How do these moire localized modes interact with local impurities?

Electronic structure of twisted bilayer

Local density of states



Experimental local density of states



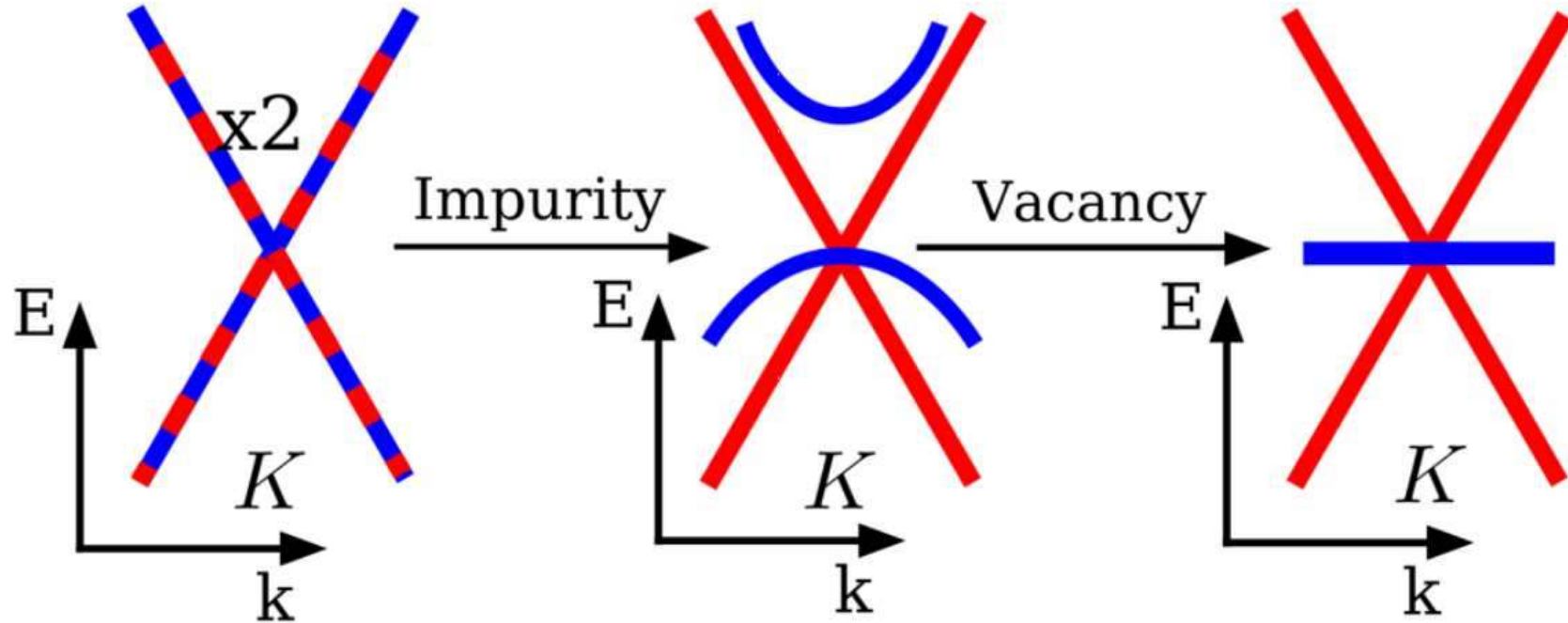
Nature Physics 6, 109–113 (2010)

Nature 572, 101–105 (2019)

Nature 572, 95–100 (2019)

How do these moire localized modes interact with local impurities?

Impact of single impurities in the twisted bilayer electronic structure



Single impurities give rise to a triple point crossing in the electronic structure

Model for impurities in twisted multilayers

Full Hamiltonian

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{W}$$

Pristine twisted bilayer graphene

$$\mathcal{H}_0 = t \sum_{\langle i,j \rangle} c_i^\dagger c_j + \sum_{i,j} \bar{t}_\perp(\mathbf{r}_i, \mathbf{r}_j) c_i^\dagger c_j$$

Intra-layer
hopping

Inter-layer
hopping

Local impurity

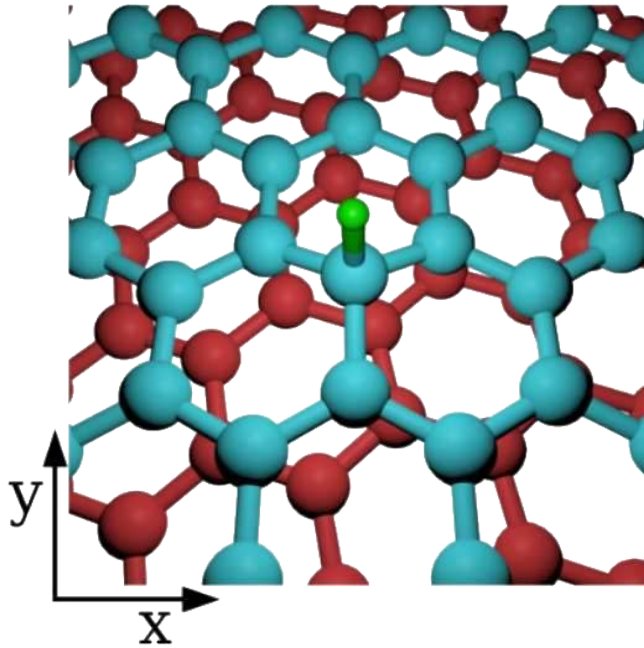
$$\mathcal{W} = w c_n^\dagger c_n$$

The limit of infinite potential corresponds to removing a site

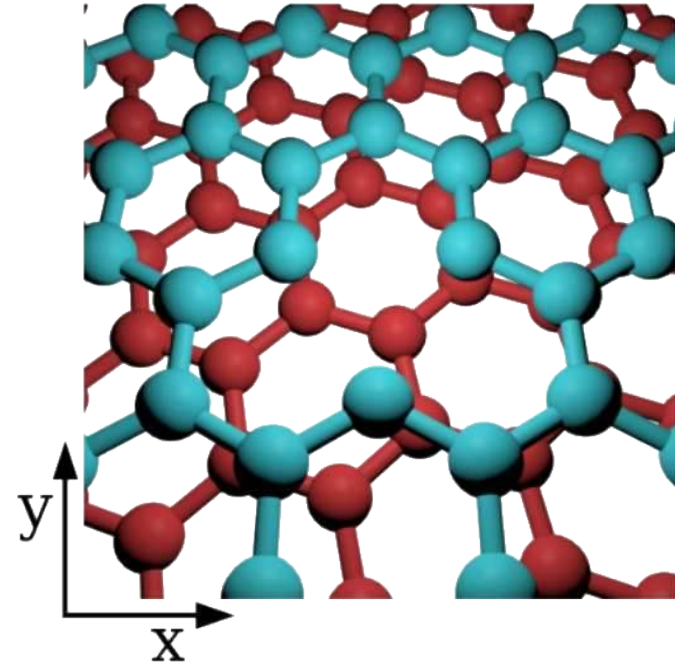
$$w \rightarrow \infty$$

The strong impurity limit

Adsorbed hydrogen in TBG



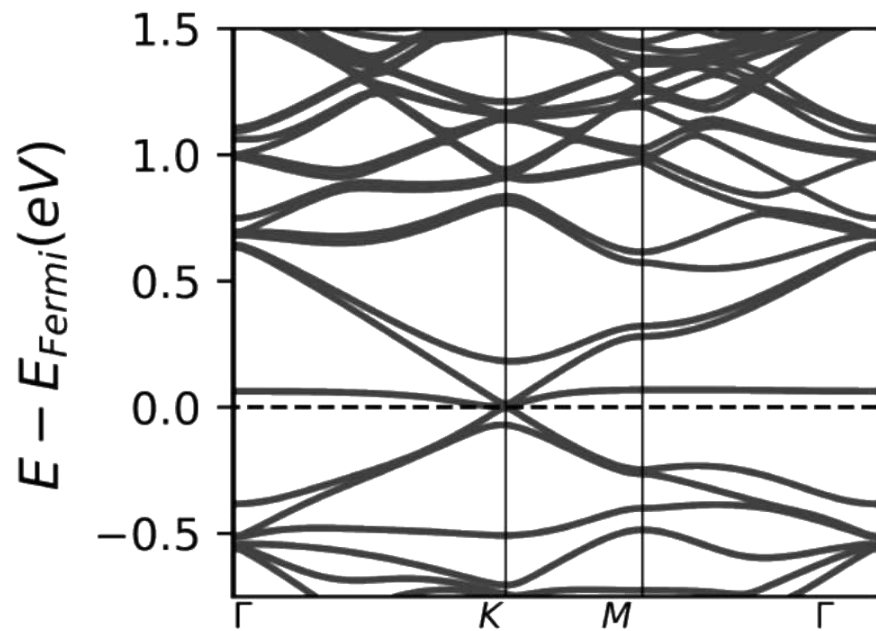
Effective tight binding model



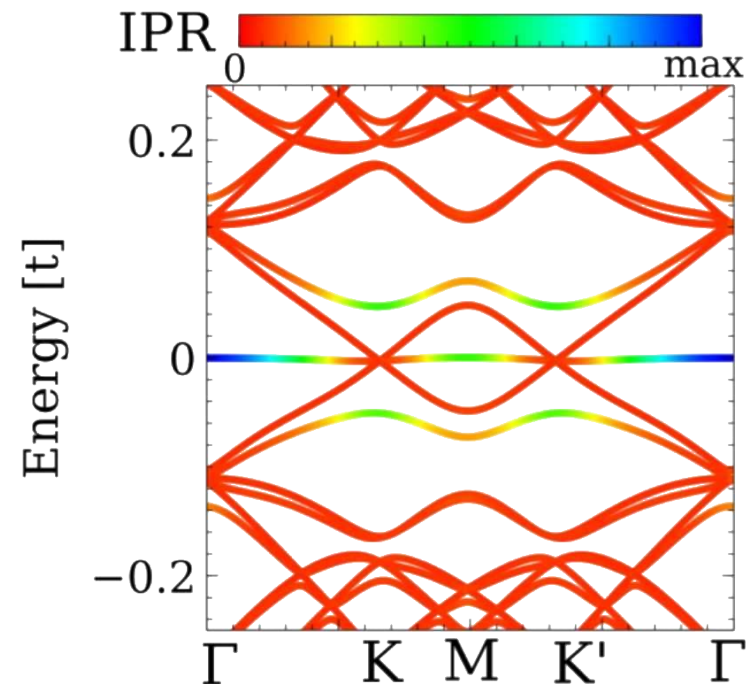
Hydrogen adsorption effectively gives rise to a vacancy in the low energy model

DFT versus tight binding

Density functional theory



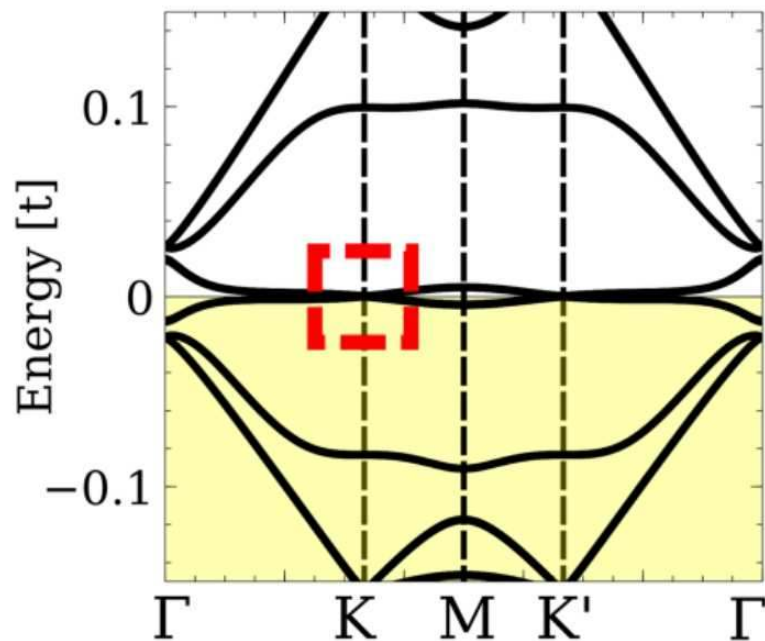
Tight binding



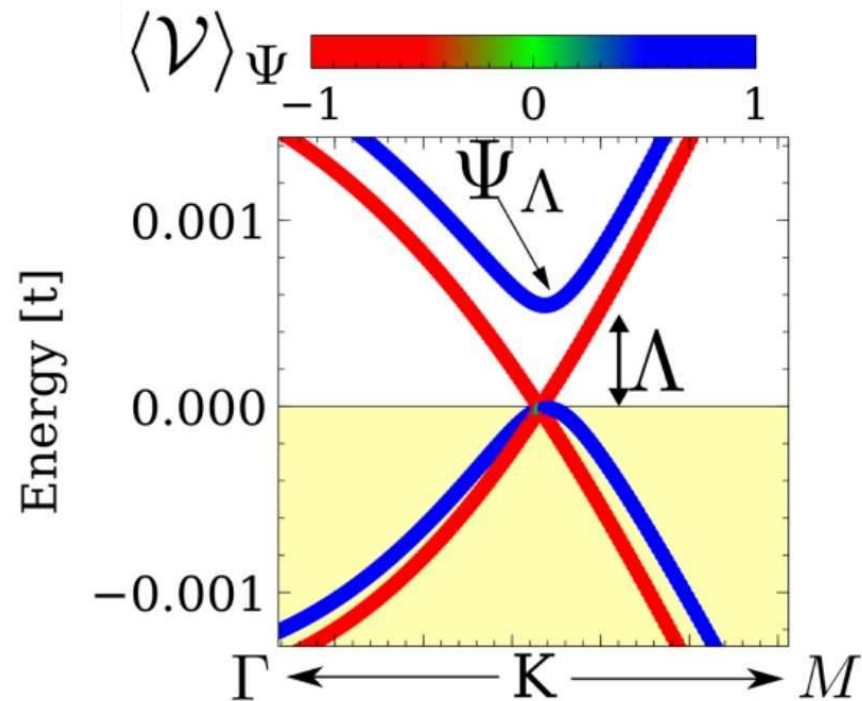
DFT and tight binding give rise to comparable electronic structures

Impact of a single weak defect

Band structure



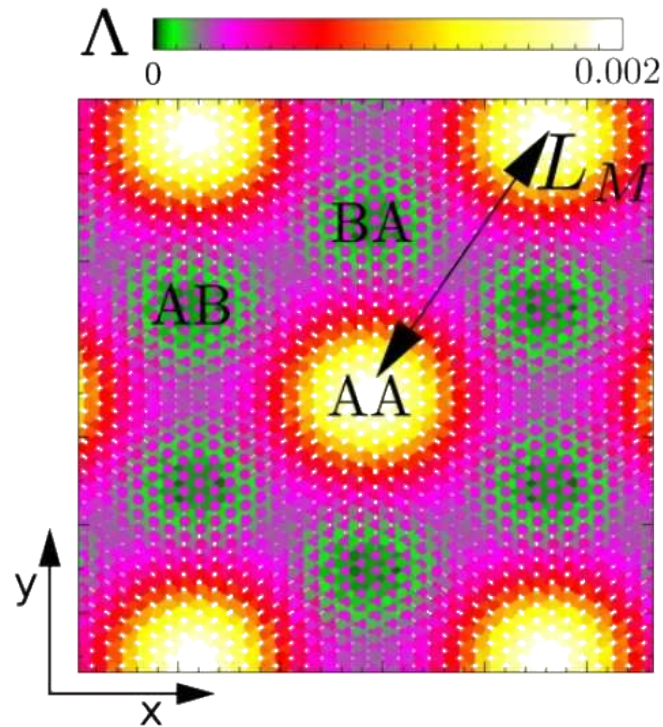
Valley expectation value



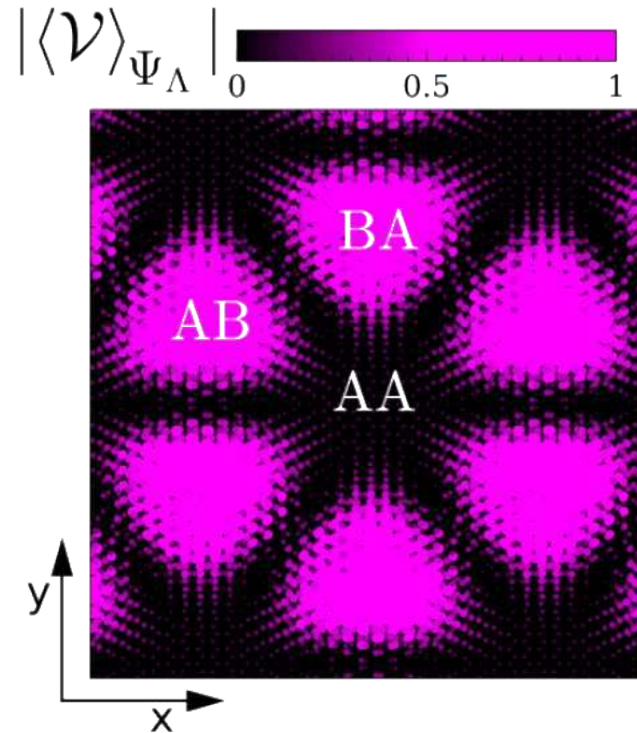
A weak impurity generates a triple band crossing at the Dirac point

Position-dependent valley mixing

Gap opening depending on the location



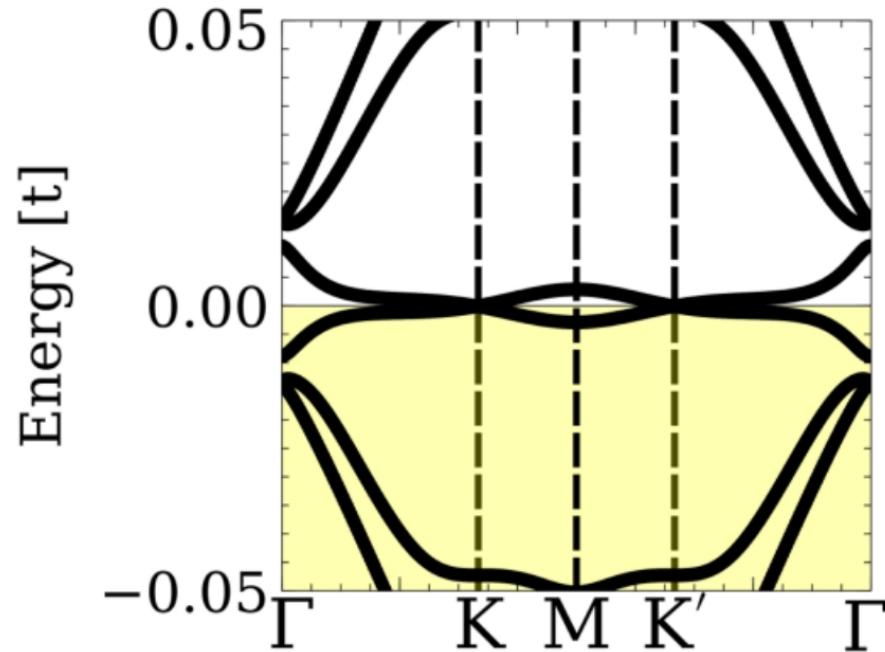
Valley polarization depending on the location



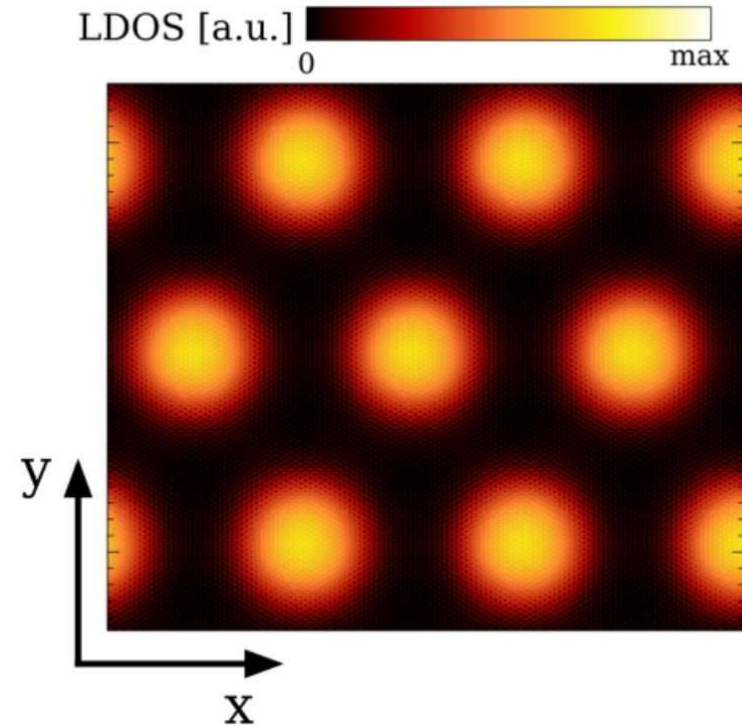
The location of the impurities determines the strength of the valley mixing

Low energy states, pristine bilayer

Band structure



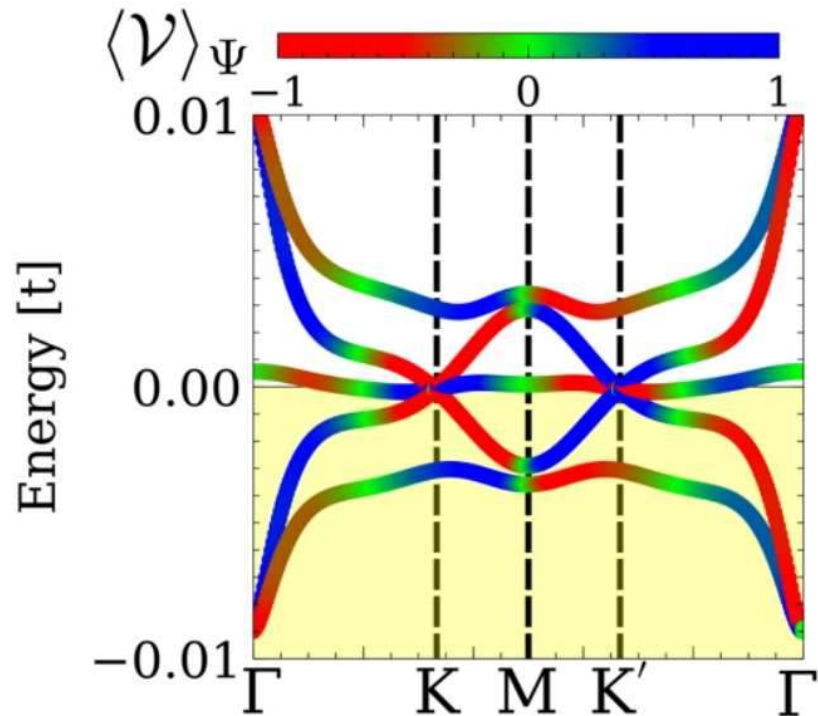
Spatial distribution of the low energy states



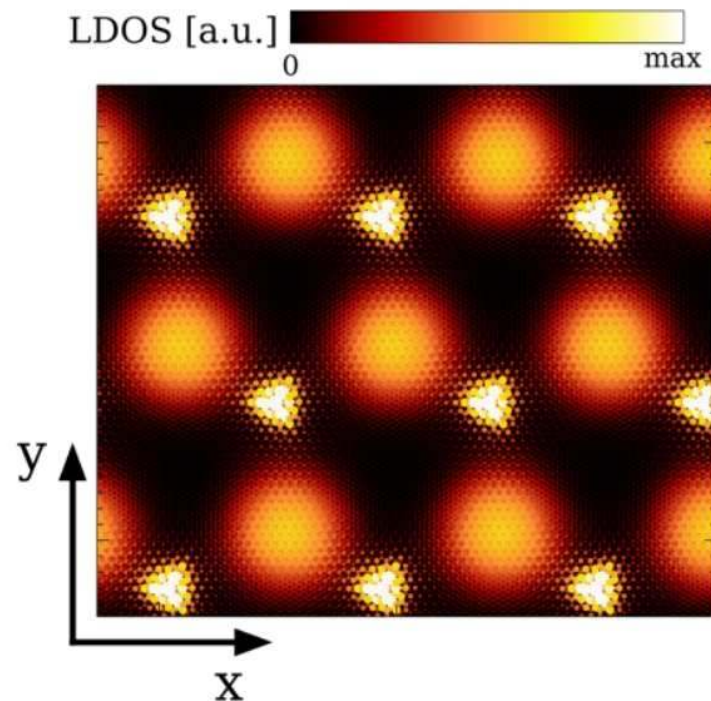
The nearly flat bands create an emergent triangular superlattice

Low energy states, strong single defect

Band structure



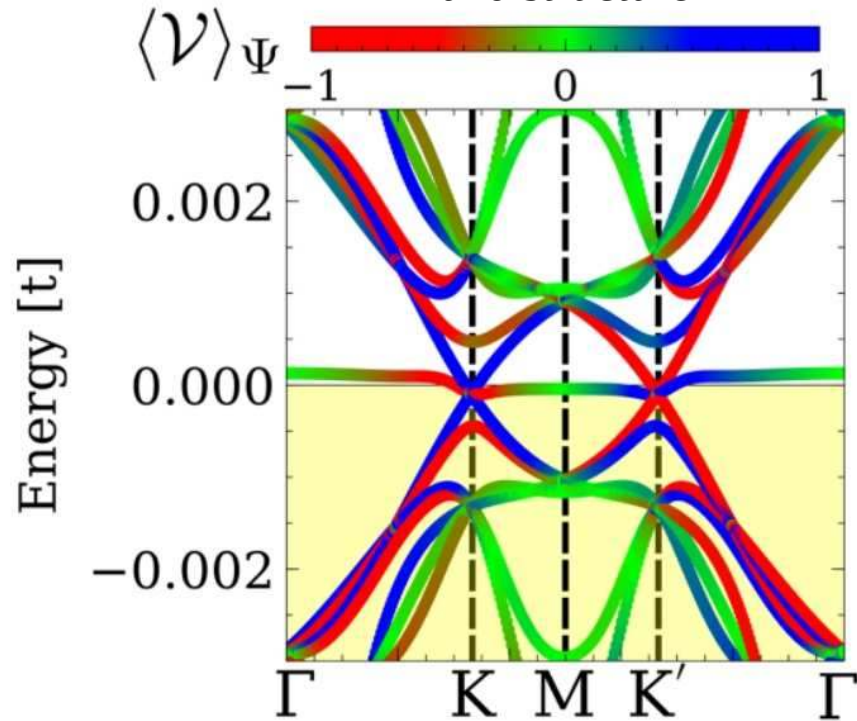
Spatial distribution of the low energy states



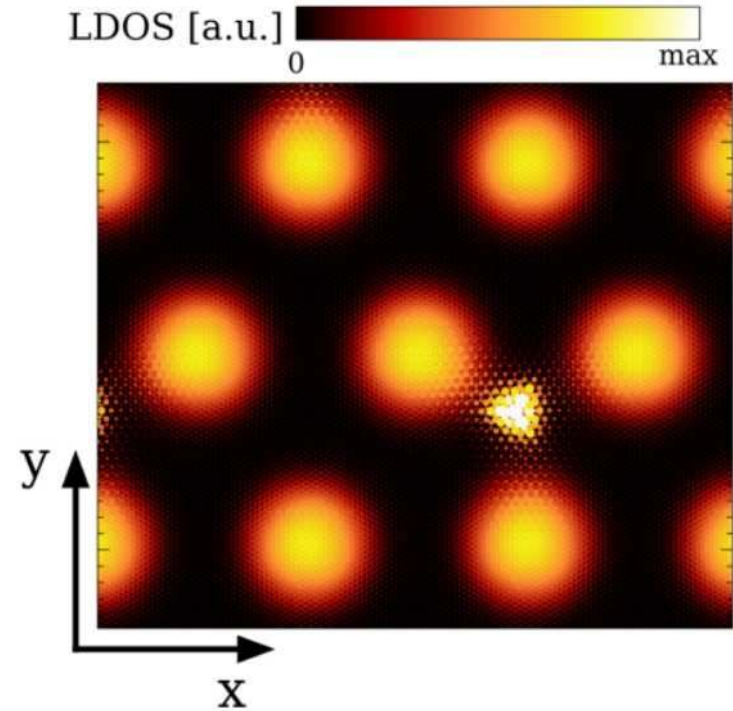
The nearly flat bands coexist with a localized vacancy state

Low energy states, strong single defect in a 4x4 supercell

Band structure



Spatial distribution of the low energy states



The nearly flat bands coexist with a localized vacancy state

Including interactions in a minimal way

We will include interactions with a minimal Hubbard repulsion

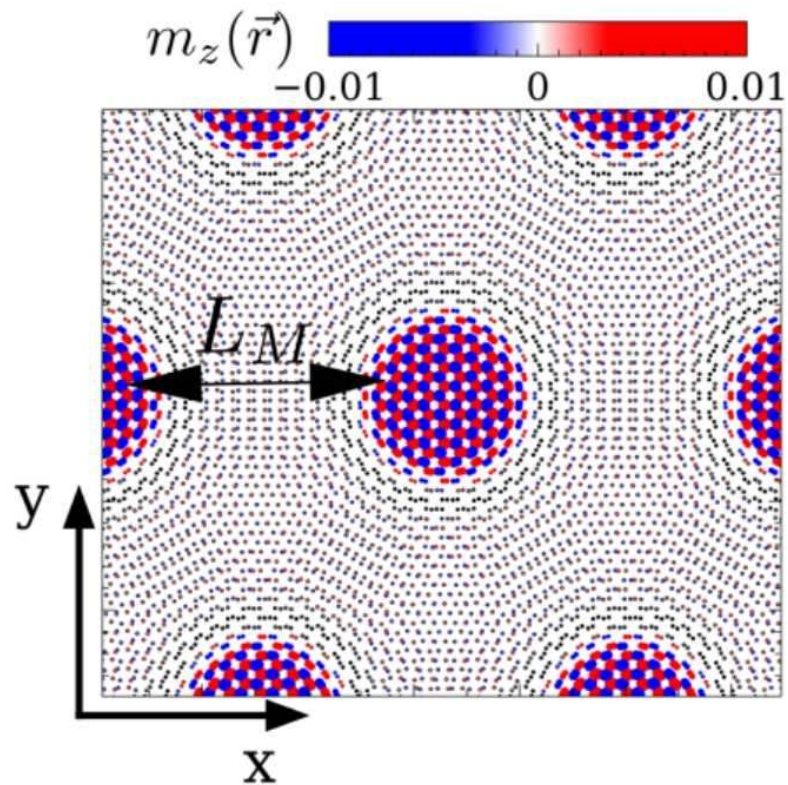
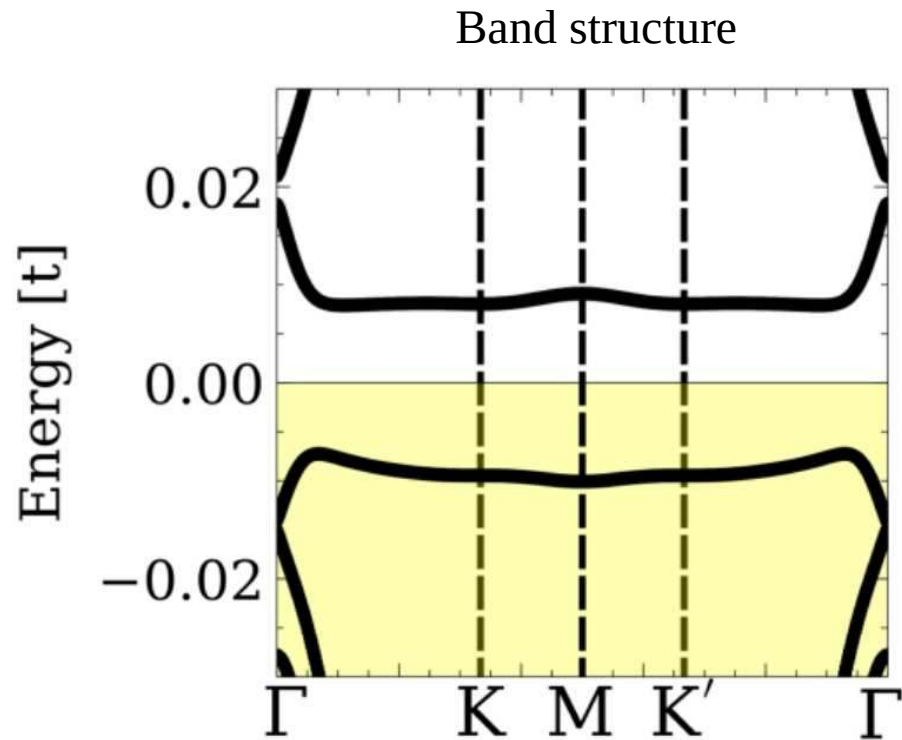
$$H_U = \sum_i U c_{i,\uparrow}^\dagger c_{i,\uparrow} c_{i,\downarrow}^\dagger c_{i,\downarrow} = \sum_i U n_{i,\uparrow} n_{i,\downarrow}$$

Solved at the mean-field level

$$H_U^{\text{MF}} = \sum_i U [\langle n_{i,\uparrow} \rangle n_{i,\downarrow} + \langle n_{i,\downarrow} \rangle n_{i,\uparrow} - \langle n_{i,\uparrow} \rangle \langle n_{i,\downarrow} \rangle]$$

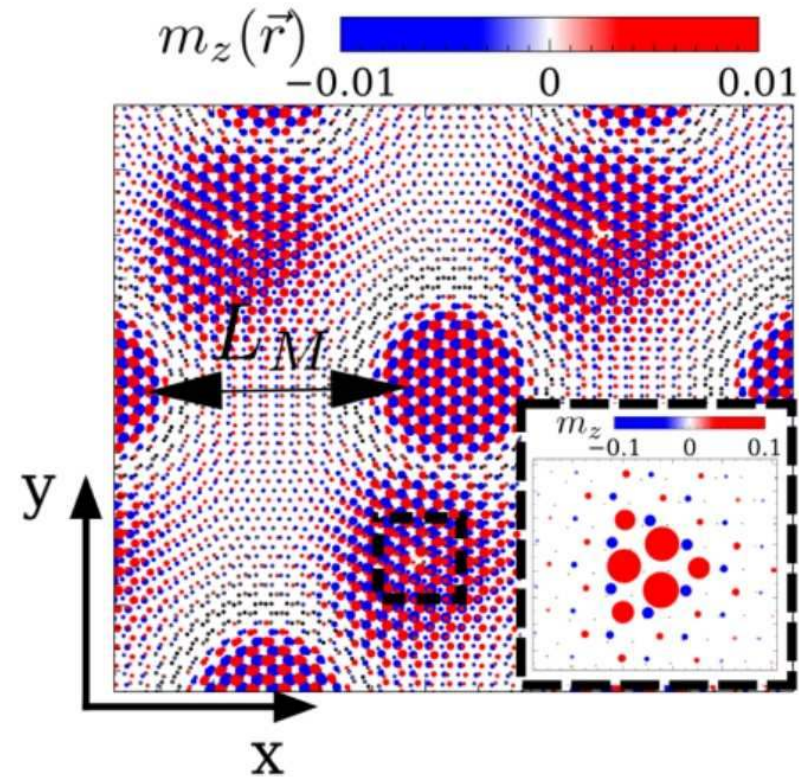
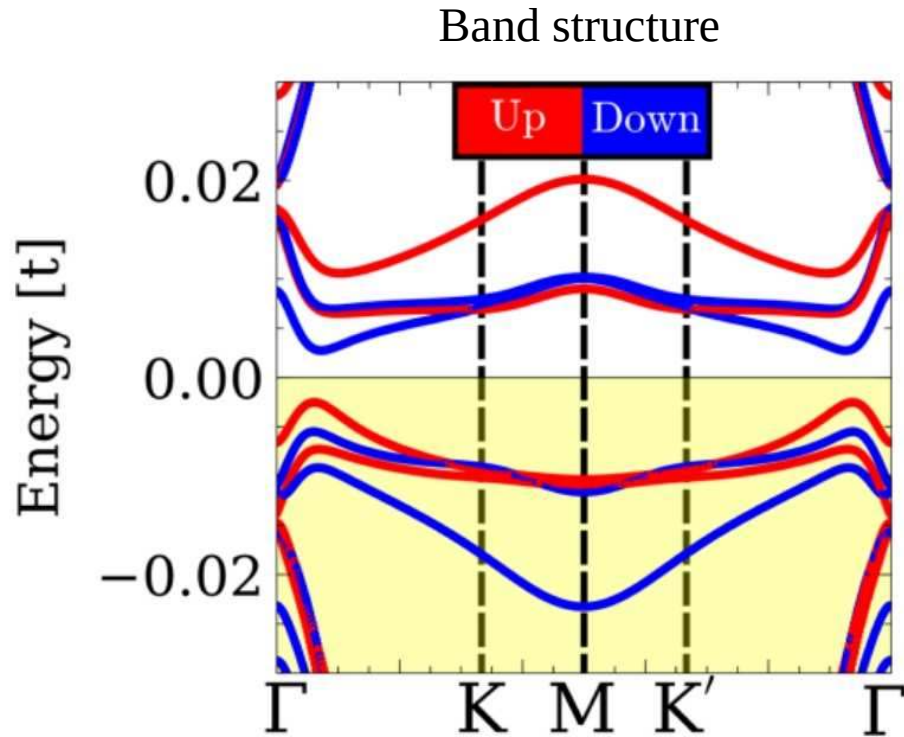
Let us see the impact on the low energy states

Impact of interactions, pristine system



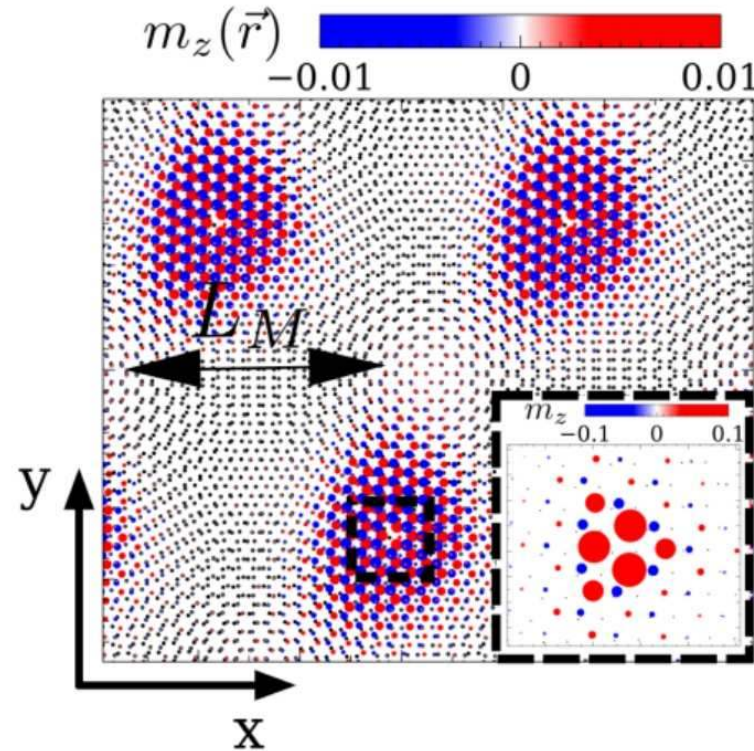
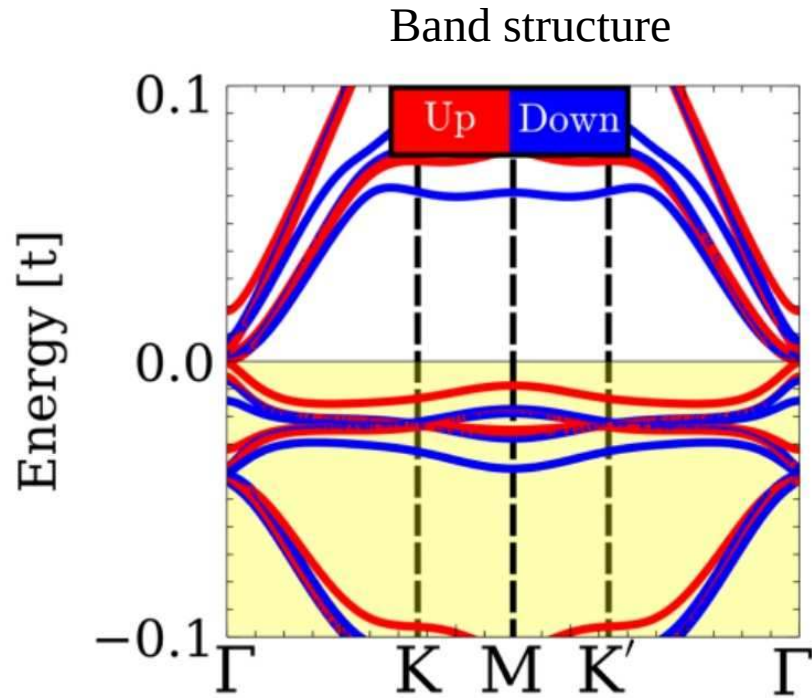
Gap opening at charge neutrality

Impact of interactions, single vacancy at charge neutrality



Interaction-driven symmetry breaking in the impurity and flat bands coexists

Impact of interactions, single vacancy at 4e per moire unit cell

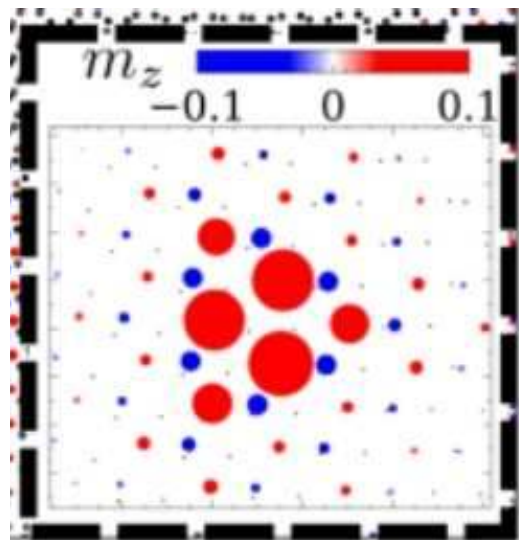


The vacancy magnetism survives full filling of the original twisted bilayer flat bands

Interplay between impurity magnetism and twisted bilayer superconductivity

The impurity induced moment survives doping of the flat bands

What happens when its magnetism coexists with the twisted bilayer superconducting state?

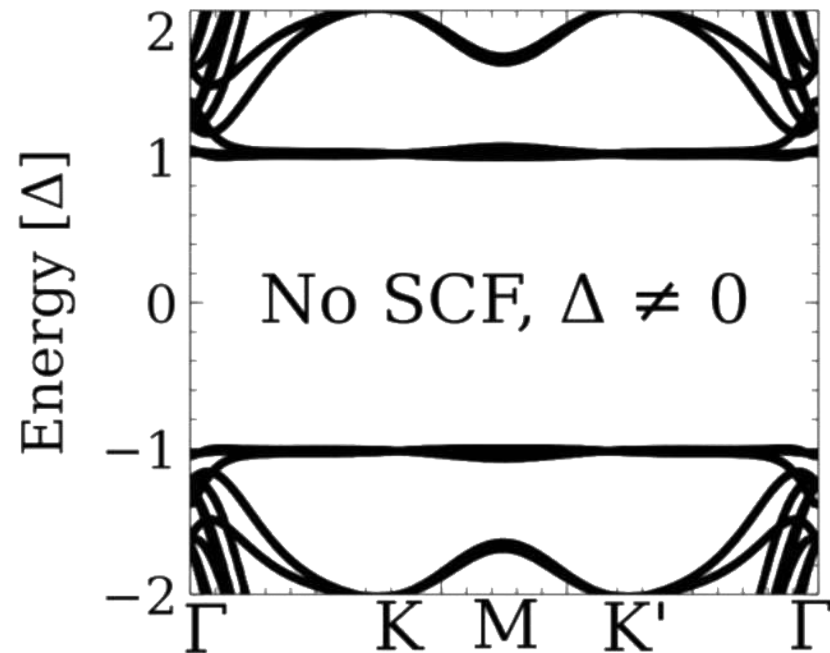
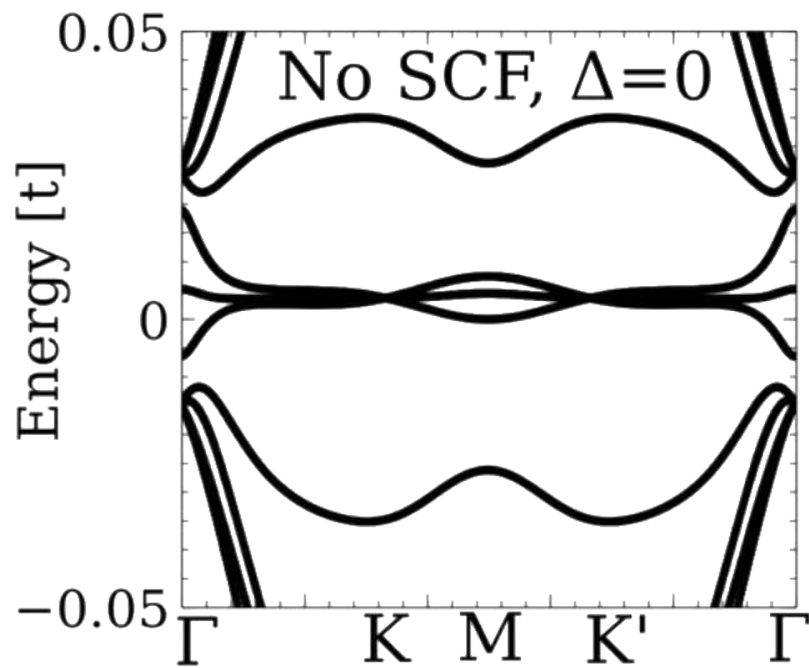


We will now include a superconducting state

$$H_{\text{SC}} = \sum_i \Delta_i [c_{i,\uparrow} c_{i,\downarrow} + c_{i,\downarrow}^\dagger c_{i,\uparrow}^\dagger]$$

Working in the regime of (close to) 2 holes per moire unit cell

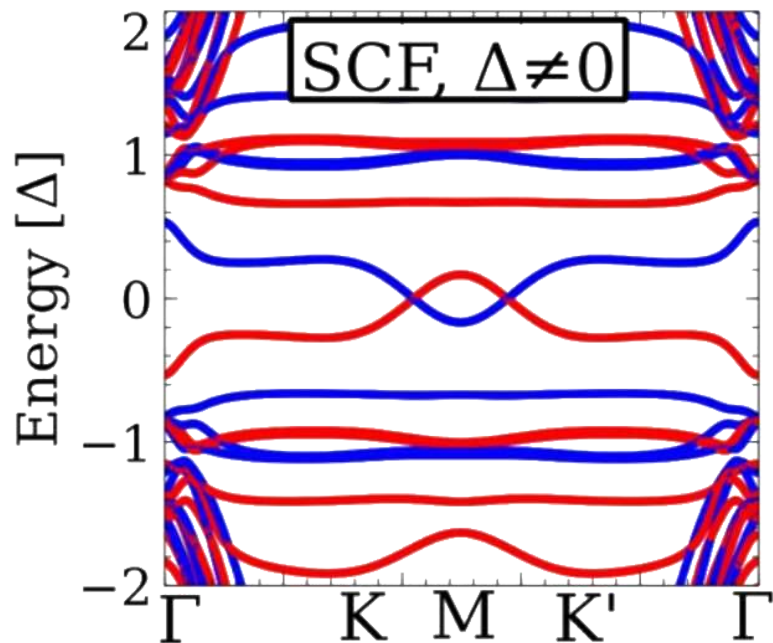
Electronic structure without including interactions



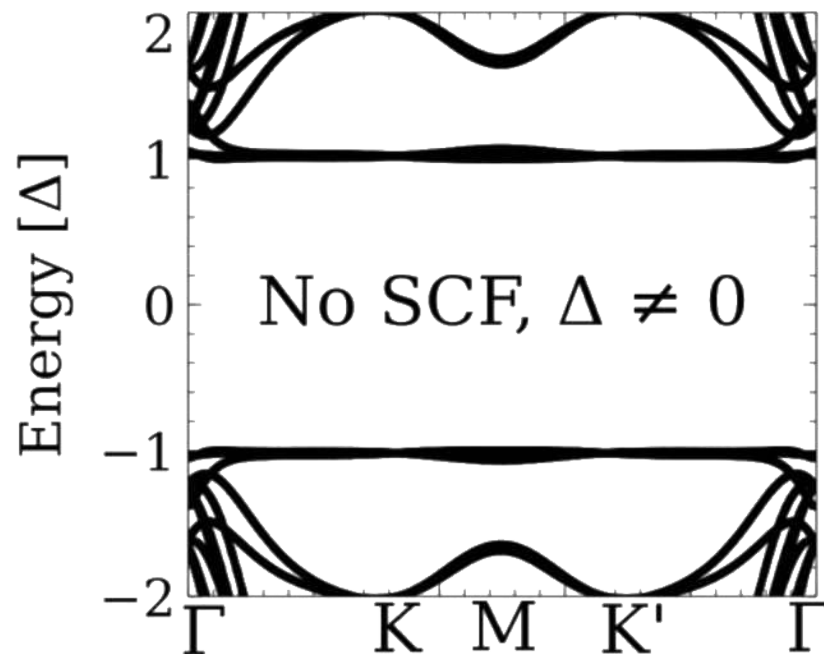
s-wave superconductivity opens up a gap in the electronic spectra

Electronic structure including repulsive interactions

With interaction-induced
magnetism



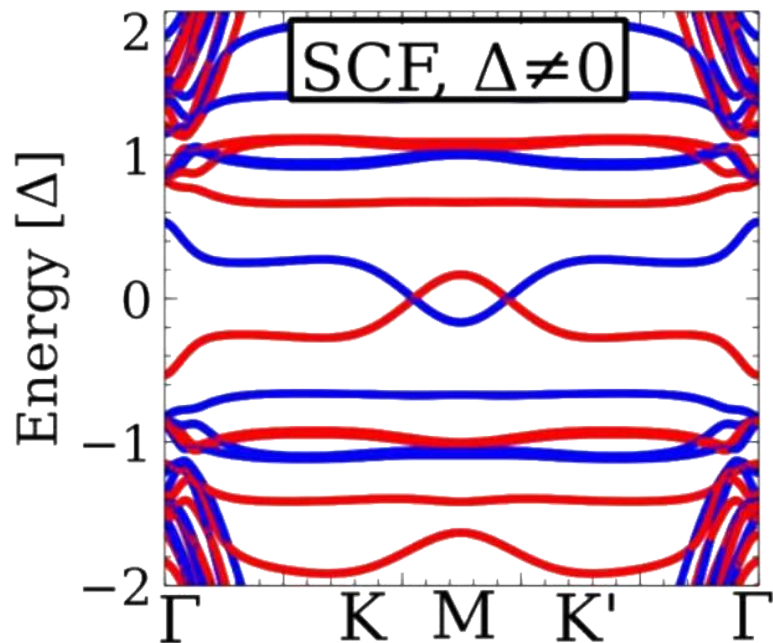
Without interaction-induced
magnetism



Impurity-induced magnetism and s-wave superconductivity gives rise to in-gap Yu-Shiba-Rusinov states

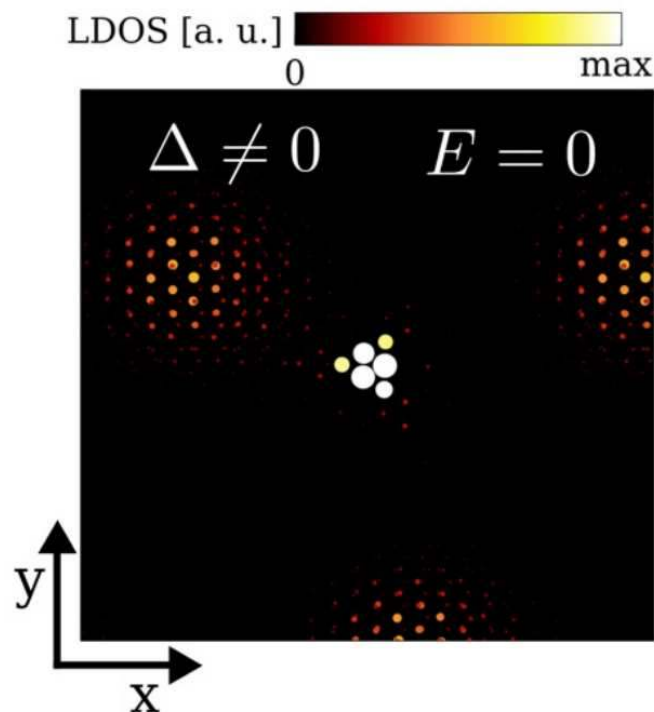
Electronic structure including repulsive interactions

With interaction-induced
magnetism



In-gap modes appear around the interaction-induced impurity magnetic moment

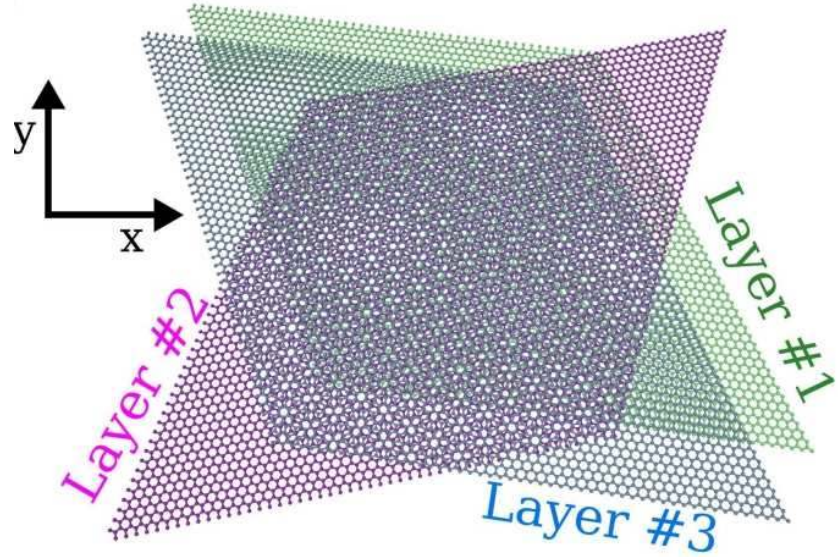
Spatial distribution of the
in-gap YSR states



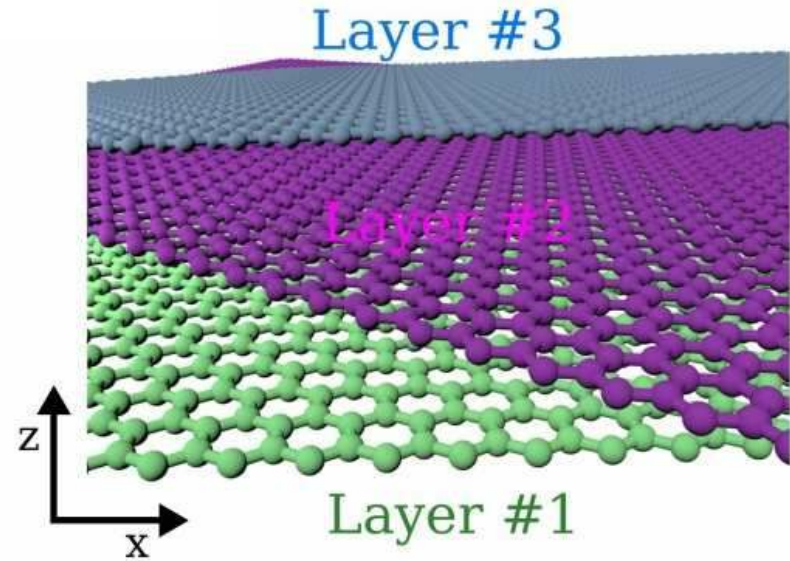
Impurities in twisted trilayer graphene

Structure of mirror-symmetric twisted graphene trilayer

Top view

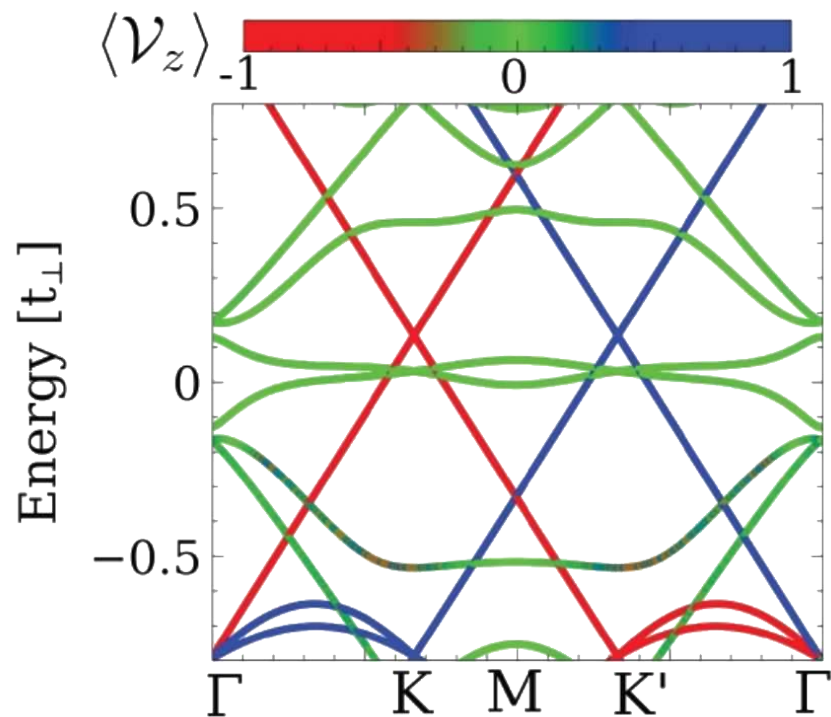


Lateral view

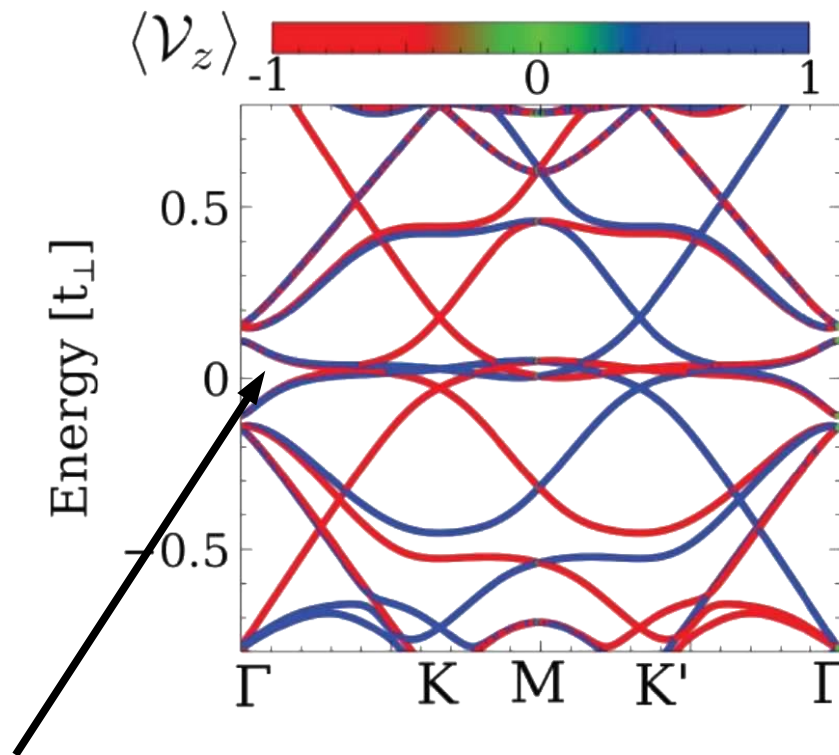


Electronic structure of twisted trilayer

Without an interlayer bias



With an interlayer bias



An interlayer bias creates internal topological valley currents

Internal topological valley currents in a twisted trilayer

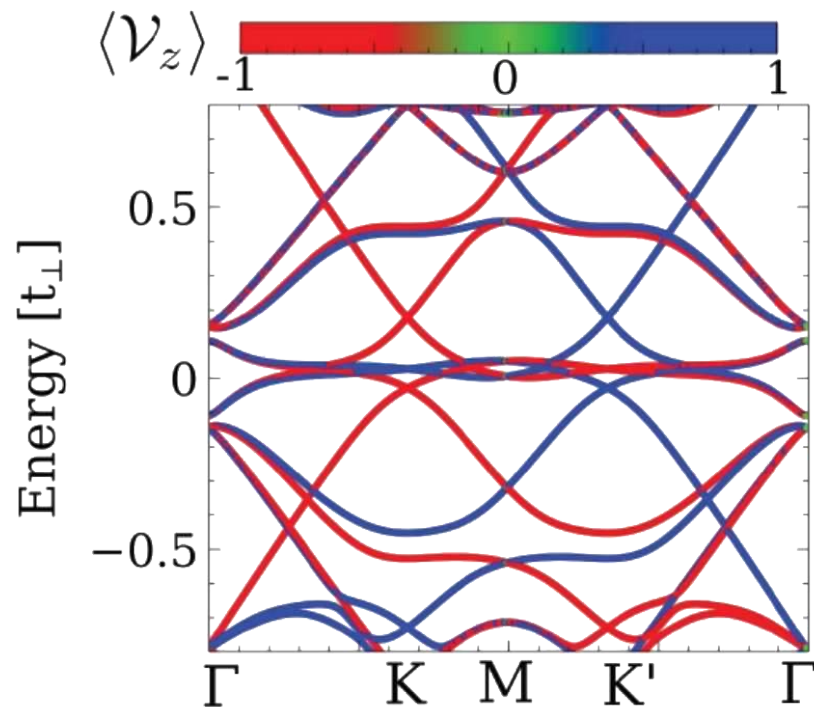
The spatially resolved valley current is defined from the valley Chern number

$$C_V = C_K - C_{K'} = \int \chi_V(\mathbf{r}, \omega) d^2\mathbf{r} d\omega$$

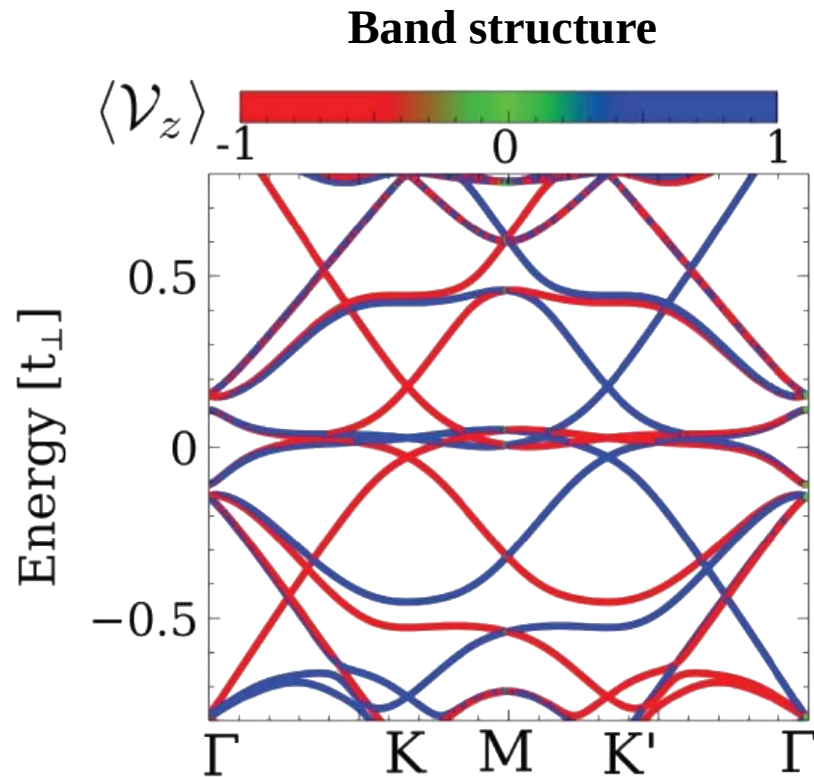
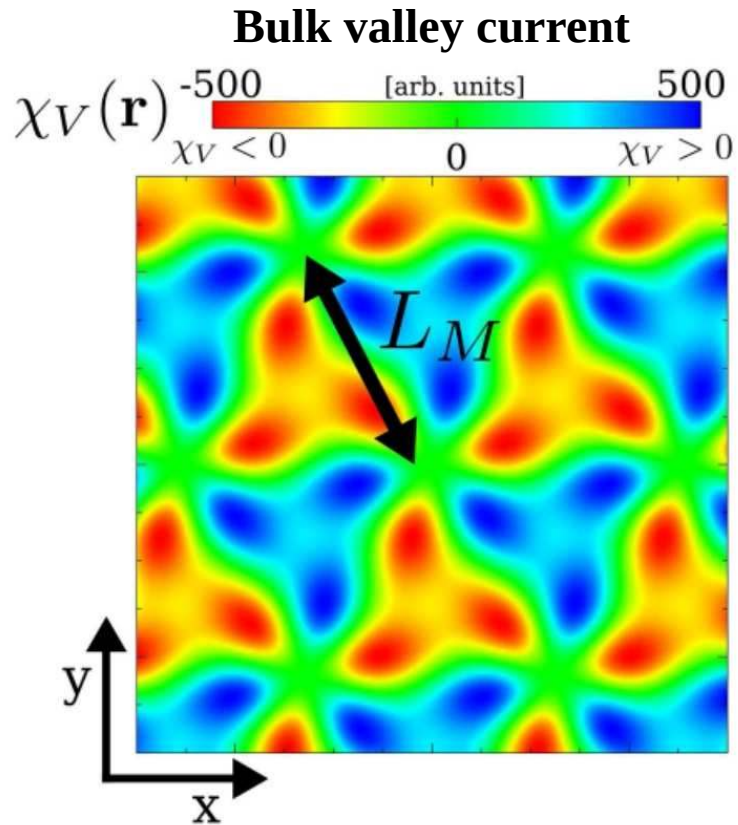
Spatially and frequency resolved valley Chern density

$$\chi_V(\mathbf{r}, \omega)$$

It represents bulk valley currents

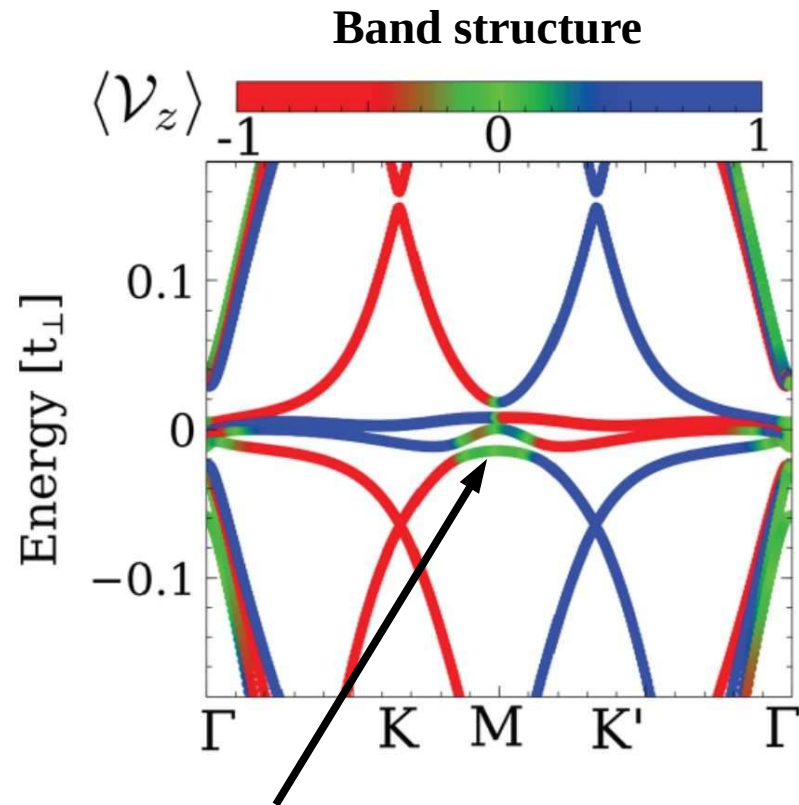
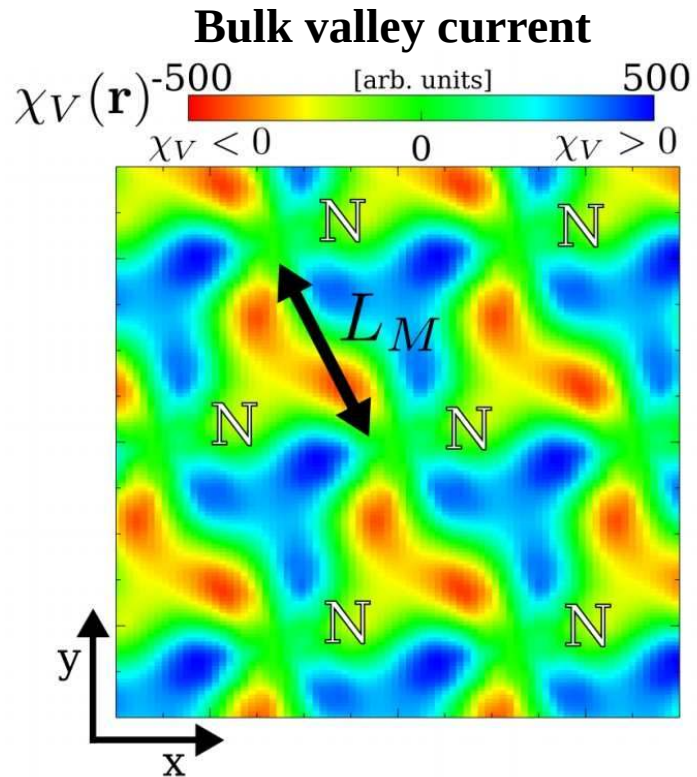


Internal topological valley currents in a twisted trilayer



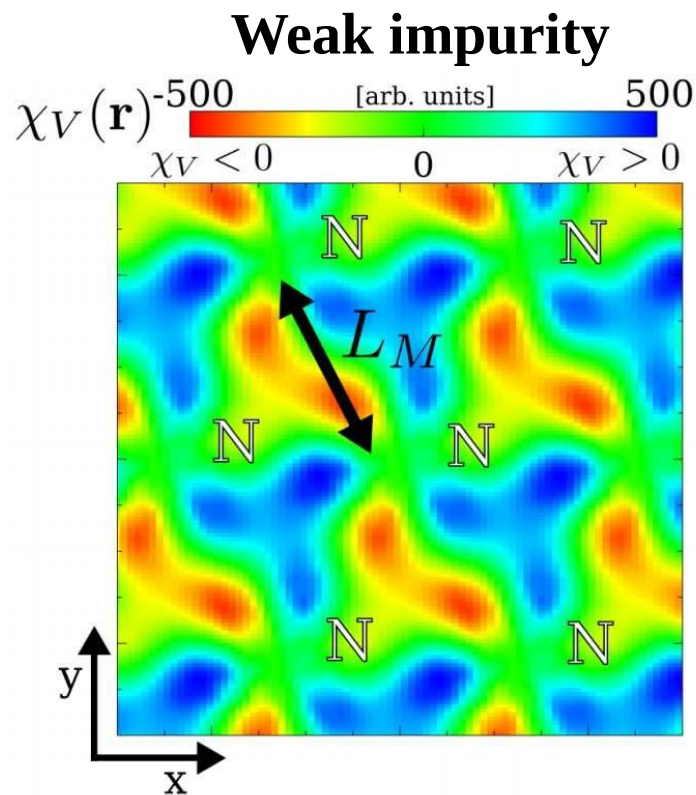
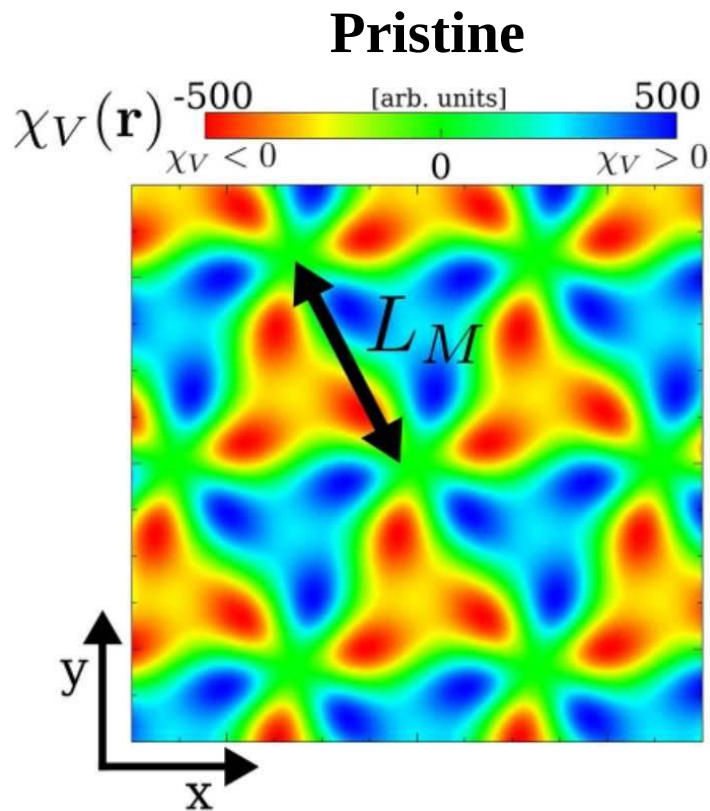
Internal topological valley currents emerge in the moire supercell

Weak impurity in a twisted graphene trilayer



Weak impurities give rise to valley mixing at low energies

Disruption of valley currents by an impurity

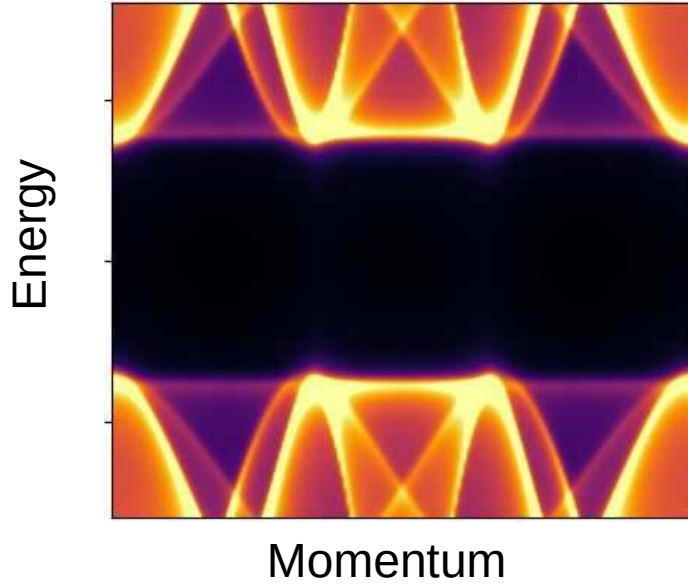


Weak impurities disrupt the valley currents in twisted graphene trilayers

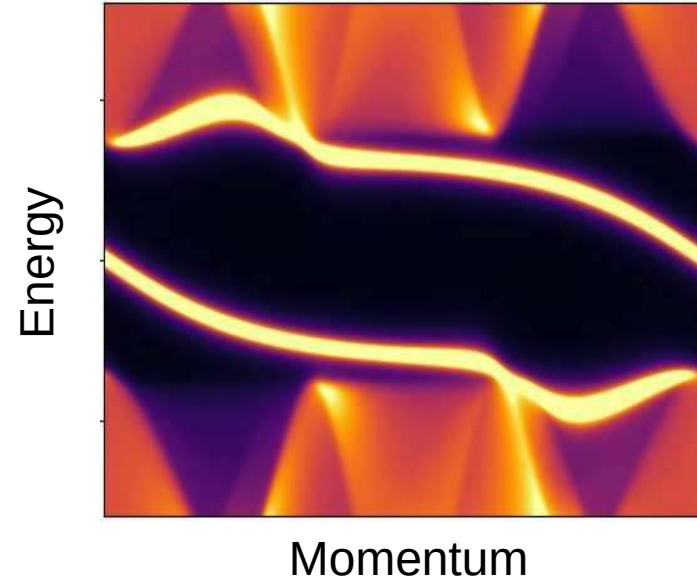
Impurities in a twisted topological superconductor

Topological superconductors

Full gap in the bulk



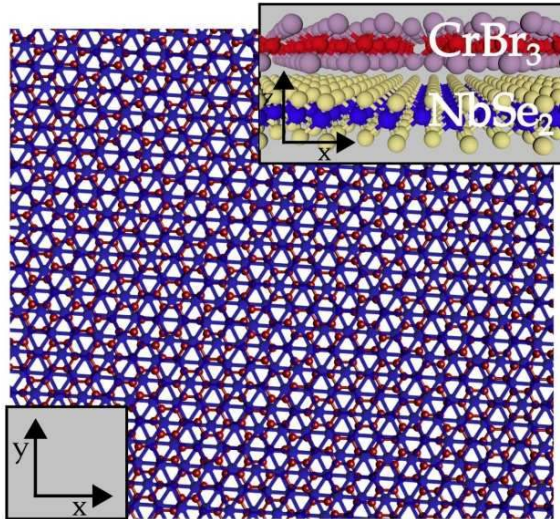
Gapless (Majorana) mode at the edge



Topological superconductors are rare in nature, and thus have to be artificially engineered

Topological superconductivity in $\text{CrBr}_3/\text{NbSe}_2$ heterostructure

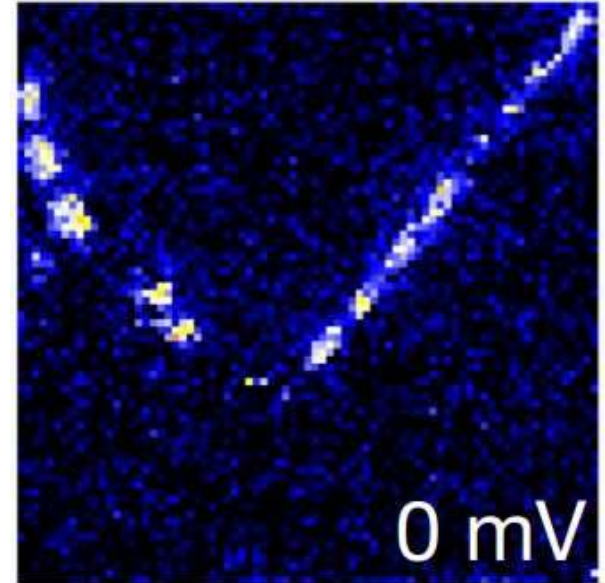
$\text{CrBr}_3/\text{NbSe}_2$ heterostructure



Nature 588, 424–428 (2020)

Nano Lett. 2022, 22, 1, 328–333

Zero bias dI/dV

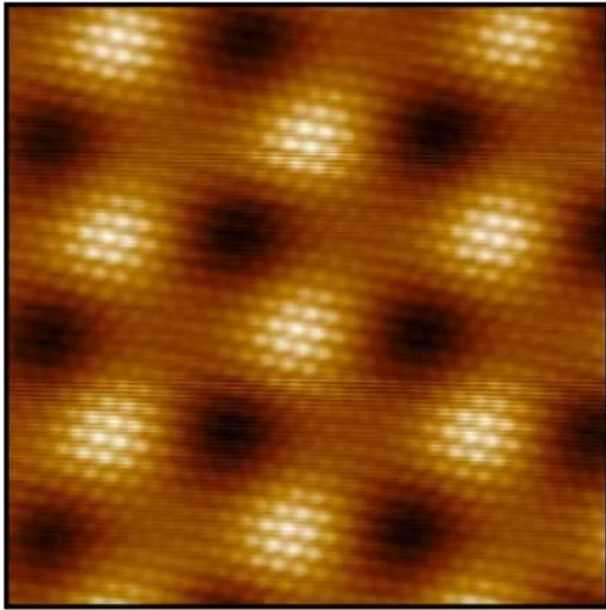


A topological superconducting state appears in $\text{CrBr}_3/\text{NbSe}_2$

$\text{CrBr}_3/\text{NbSe}_2$ heterostructure

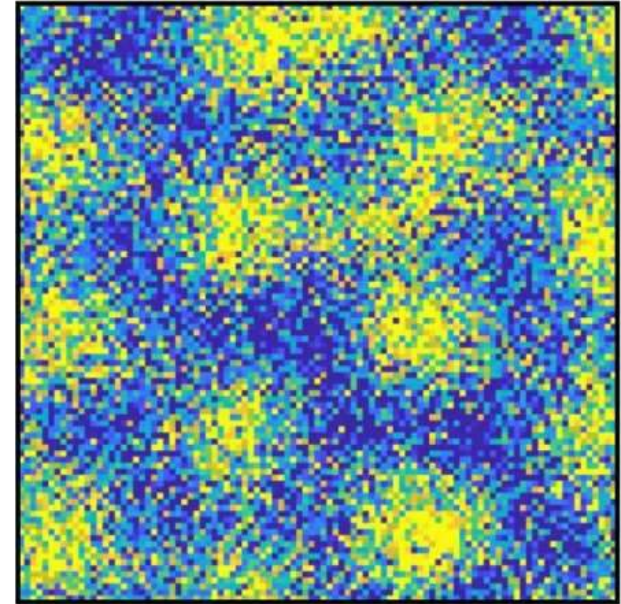
Topography

Height 0 Å 0.26 Å



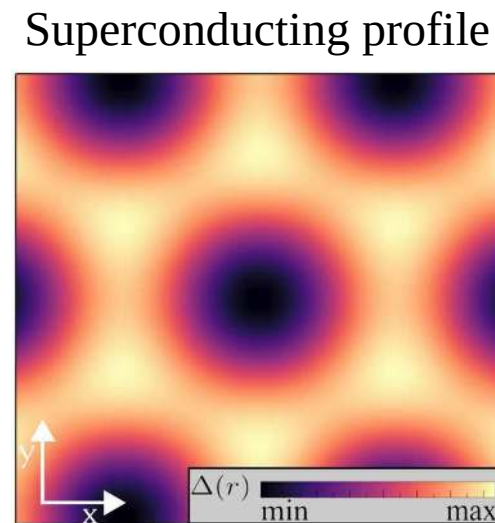
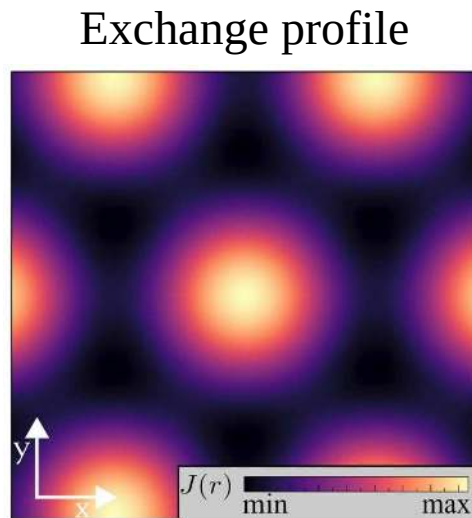
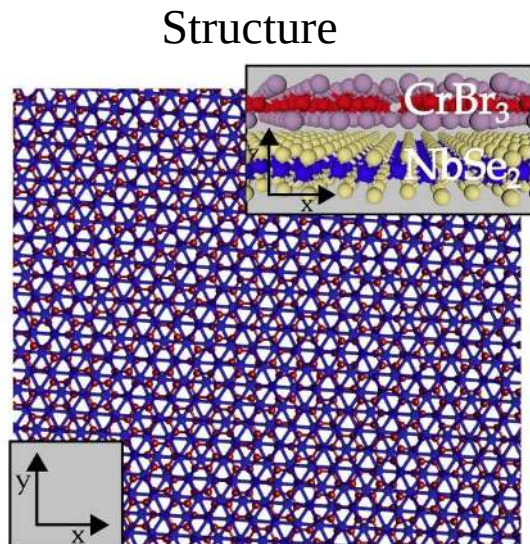
dIdV of the Yu-Shiba-Rusinov states

dI/dV (nS) 36 49



The low energy properties are affected by the moiré pattern

Hamiltonian for the pristine moire topological superconductor



$$\mathcal{H}_0 = \mathcal{H}_{\text{kin}} + \mathcal{H}_J + \mathcal{H}_R + \mathcal{H}_{\text{SC}}$$

Kinetic
energy

Exchange
coupling

Rashba
SOC

s-wave
superconductivity

Hamiltonian for the defective moire topological superconductor

Full Hamiltonian

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_{\text{imp}}$$

Local impurity in the moire system

$$\mathcal{H}_{\text{imp}} = w \sum_s c_{n,s}^\dagger c_{n,s}$$

Weak impurity

$$w \rightarrow 0$$

Strong impurity

$$w \rightarrow \infty$$

$$\mathcal{H}_0 = \mathcal{H}_{\text{kin}} + \mathcal{H}_J + \mathcal{H}_R + \mathcal{H}_{\text{SC}}$$

Kinetic
energy

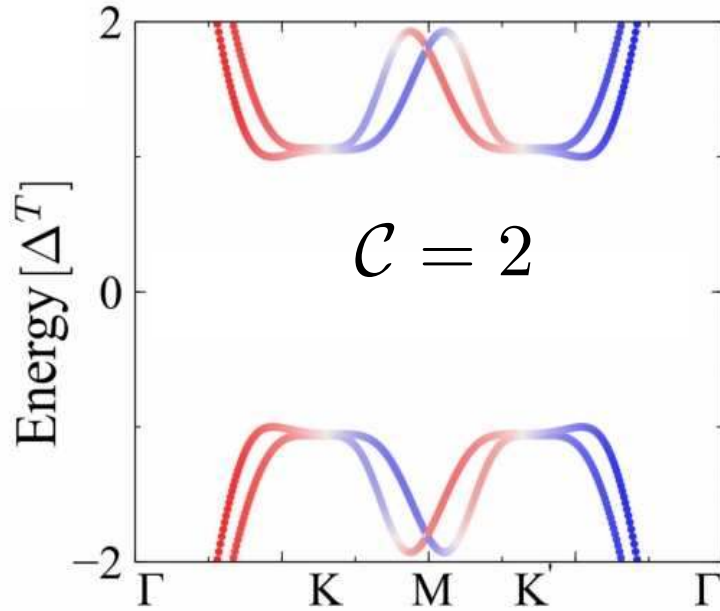
Exchange
coupling

Rashba
SOC

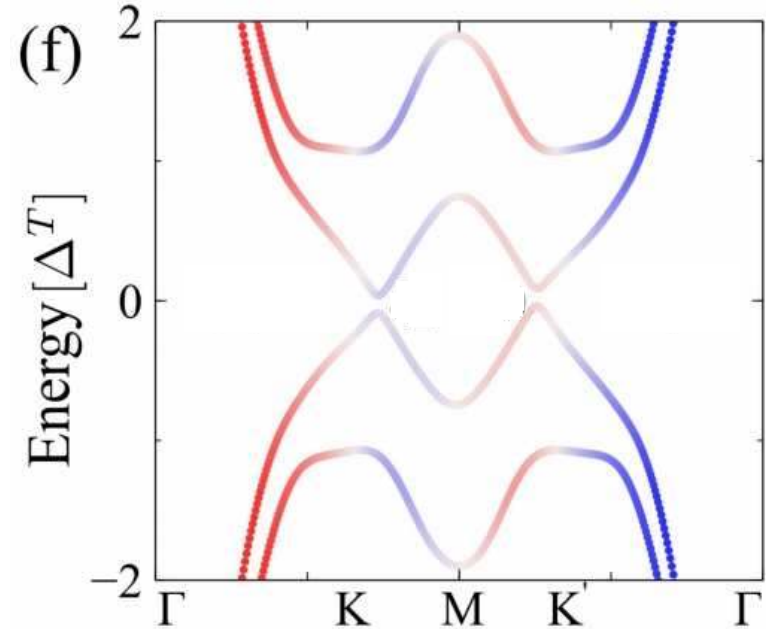
s-wave
superconductivity

Impurities in the moire topological superconductor

Band structure in the absence of impurity

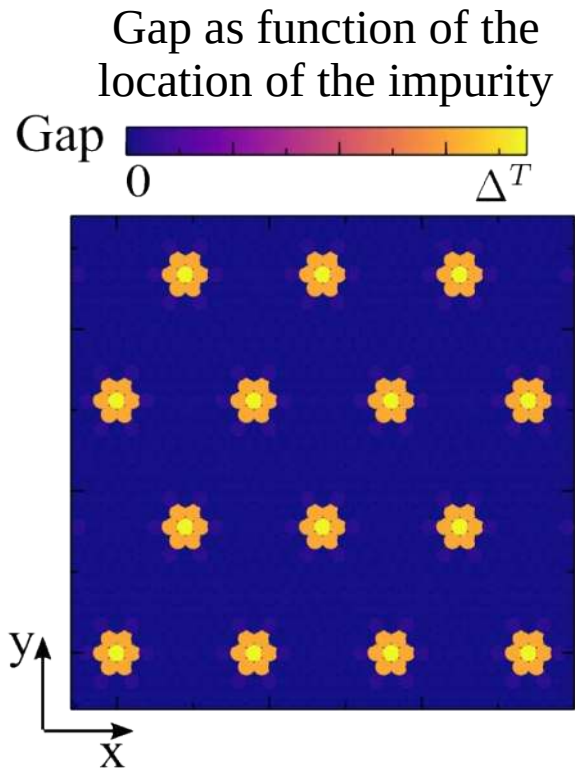


Band structure in the presence of an impurity

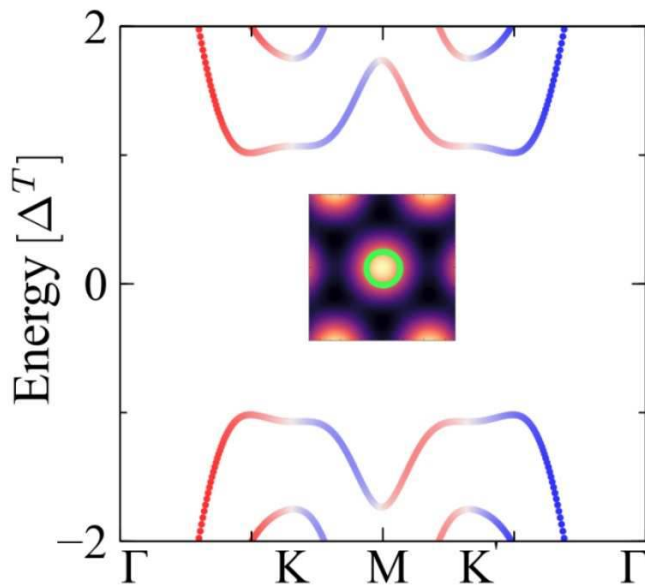


Strong local impurities decrease the size of a topological gap

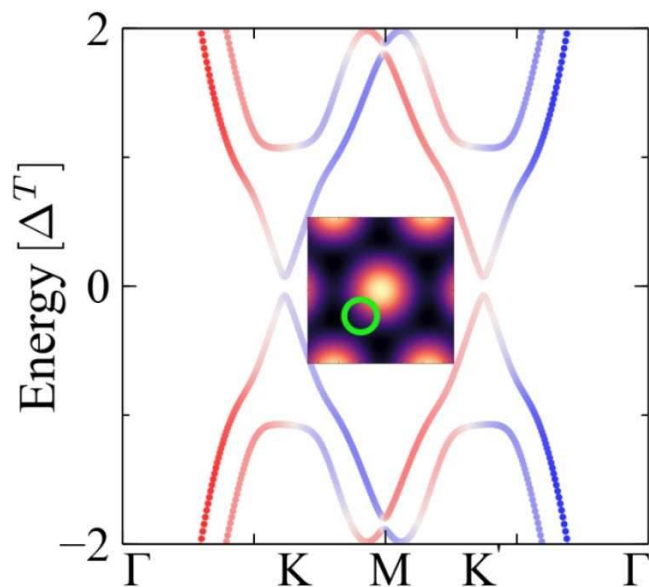
Gap as a function of the location of a strong impurity



Band structure for impurity at the center



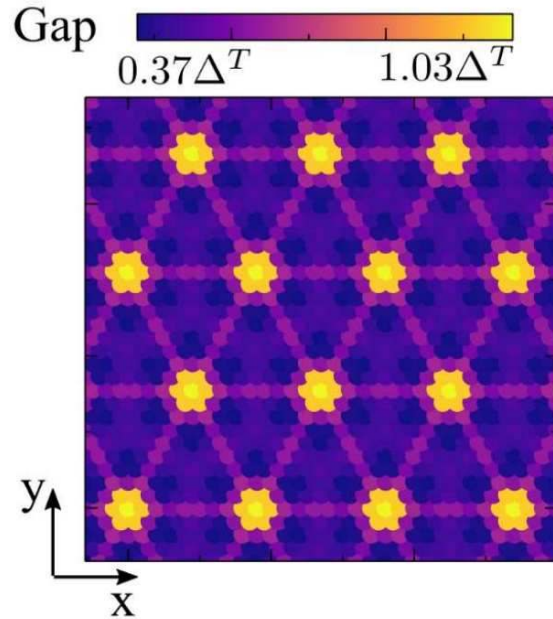
Band structure for impurity away from the center



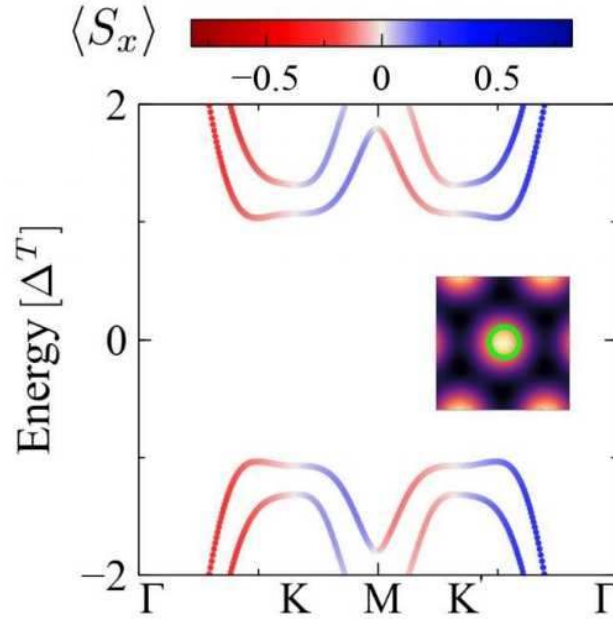
The location of the impurity strongly affects the resulting gap

Gap as a function of the location of a strong impurity

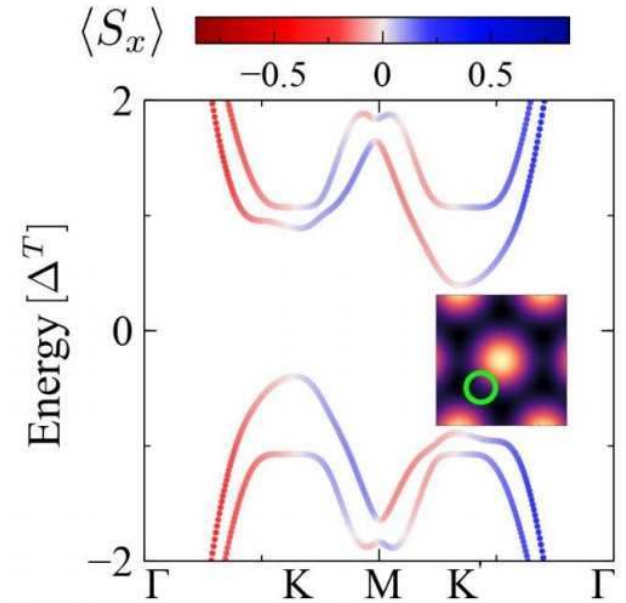
Gap as function of the location of the impurity



Band structure
for impurity at the center

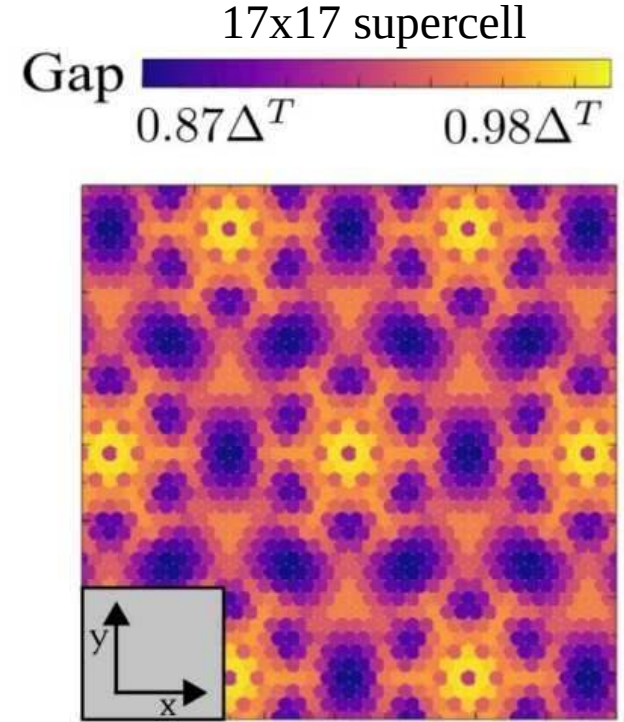
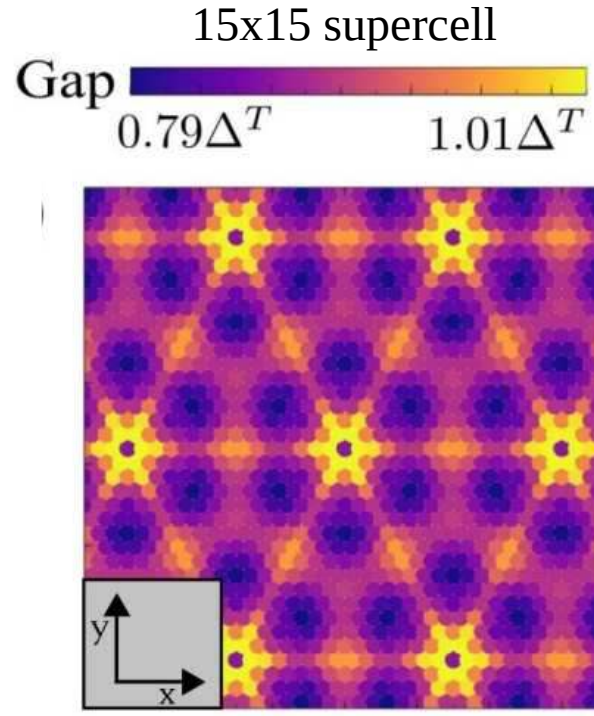
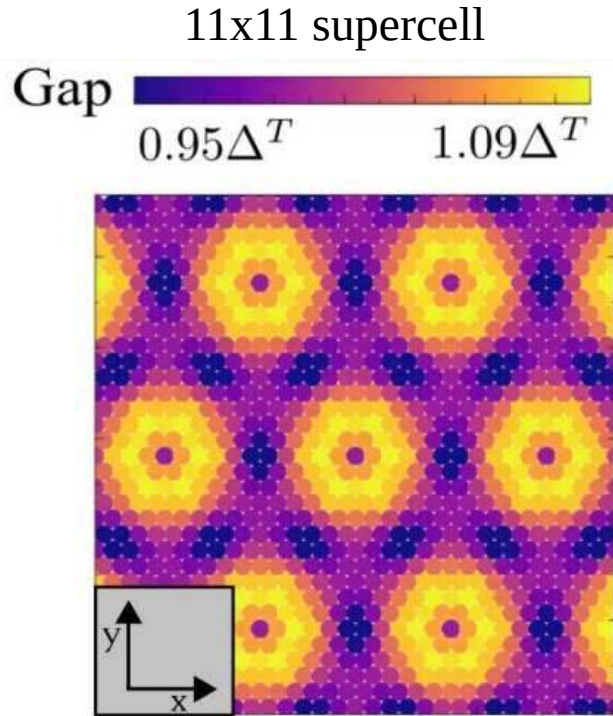


Band structure for
impurity away from the center



The location of the impurity strongly affects the resulting gap

Gap as function of location for different moire unit cells



Detrimental locations for impurities depend on the specific moire supercell

The single impurity limit

We now look at the single impurity regime

From the Green's function, we can compute the spatially resolved density of states at the energy of the YSR state

$$\rho(\mathbf{x}, \omega) = -\frac{1}{\pi} \sum_{s, \tau} \langle \mathbf{x}, s, \tau | \text{Im}(G_V(\omega)) | \mathbf{x}, s, \tau \rangle$$

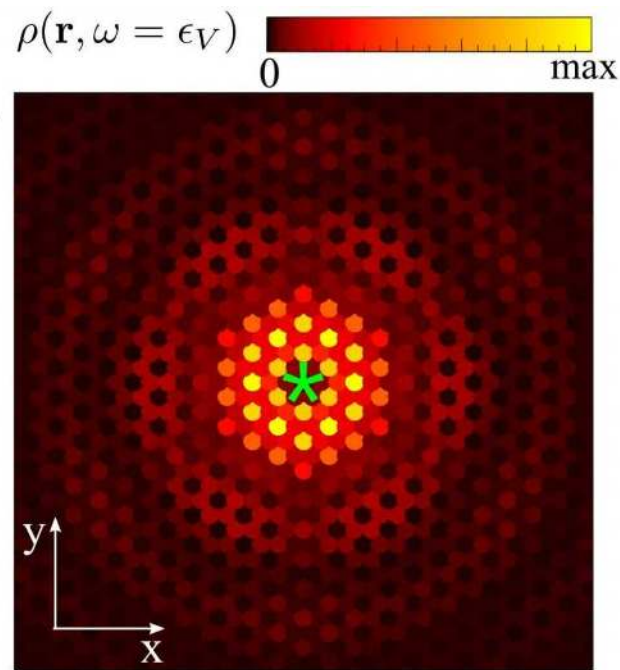
Dyson equation for a single impurity

$$G_V(\omega) = [\omega - H_V - \Sigma(\omega) + i0^+]^{-1}$$

Selfenergy from the pristine regime

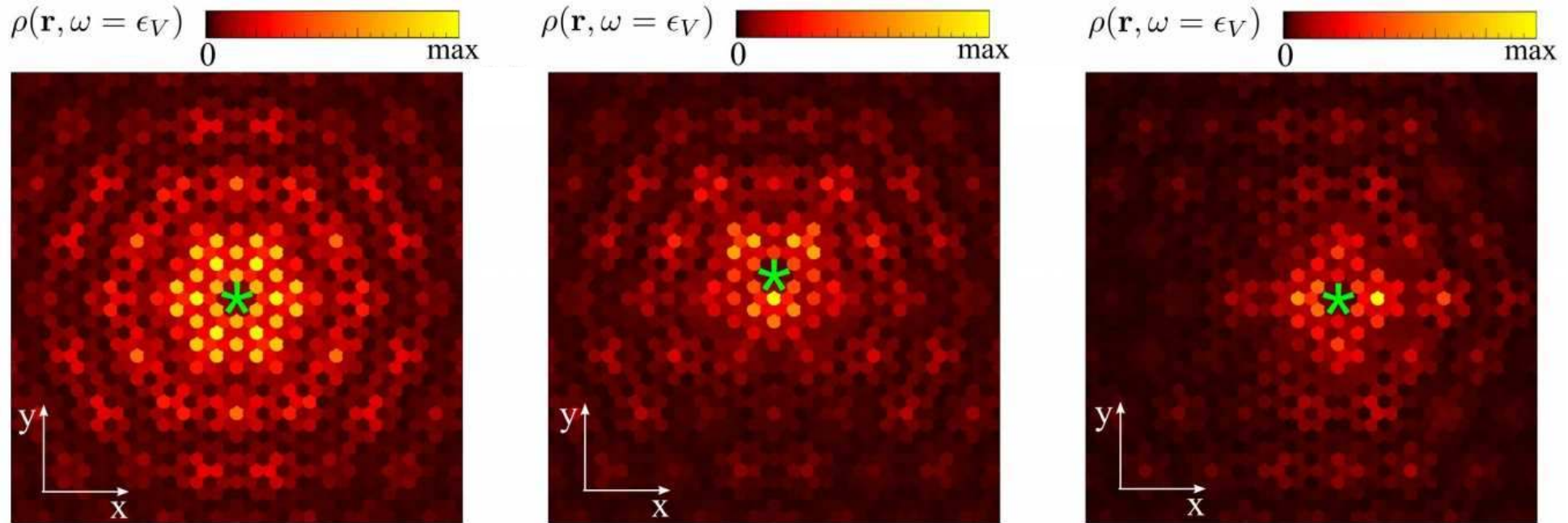
$$G_0(\omega) = [\omega - H_0 - \Sigma(\omega) + i0^+]^{-1}$$

YSR without moire



Single impurity in a topological moire superconductor

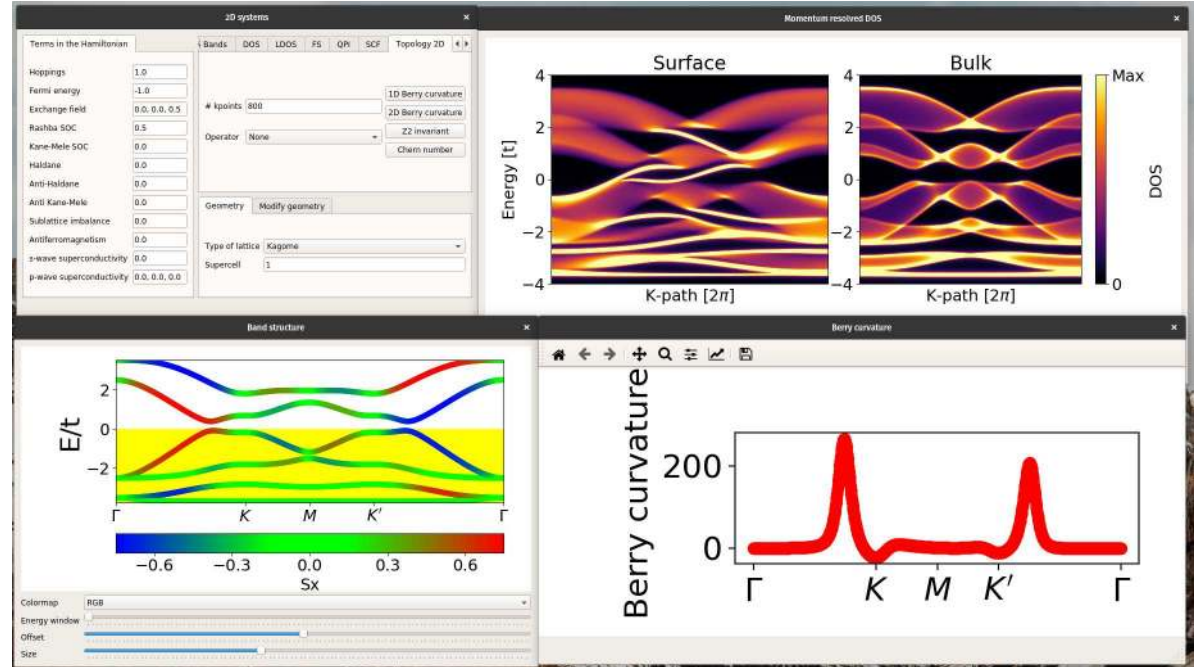
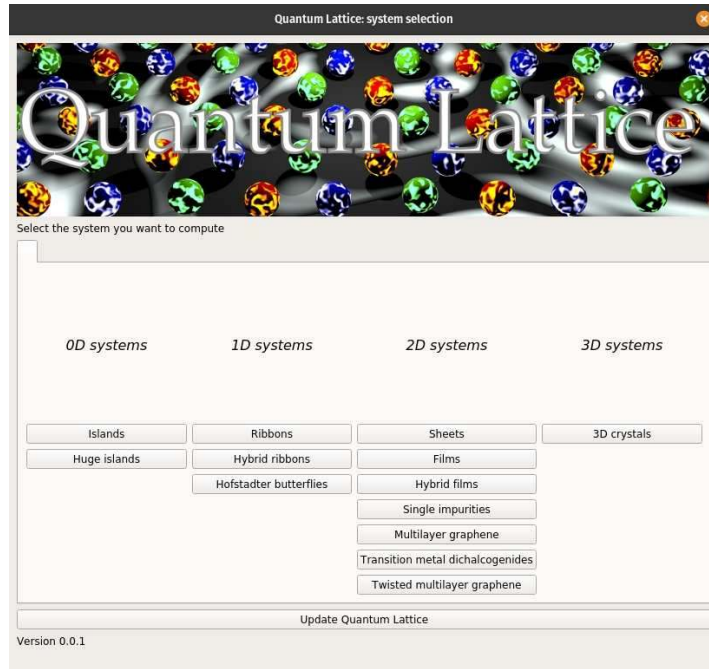
Wavefunction of the YSR state for different impurity locations



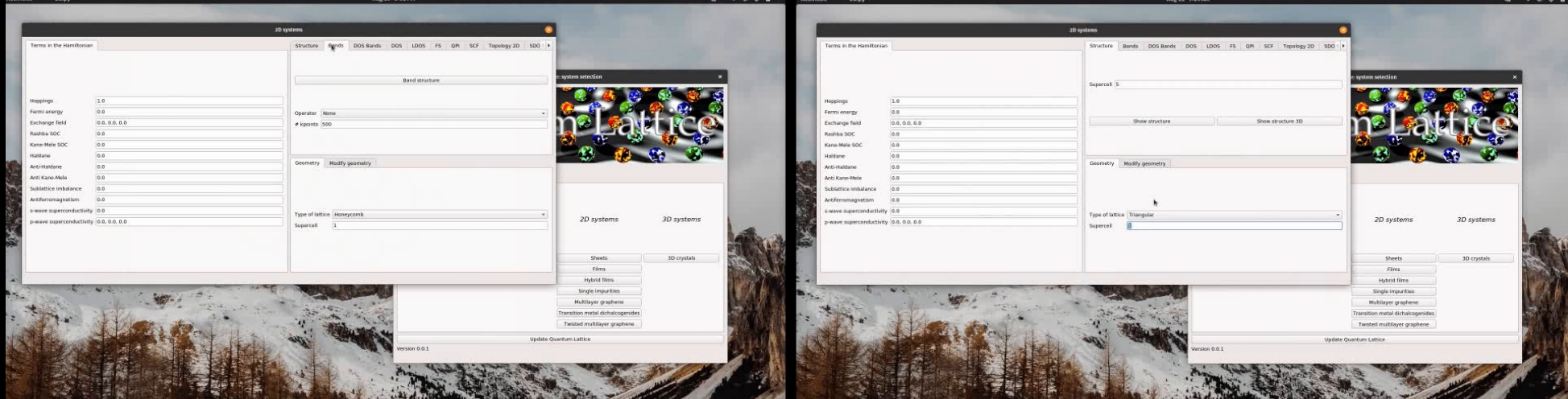
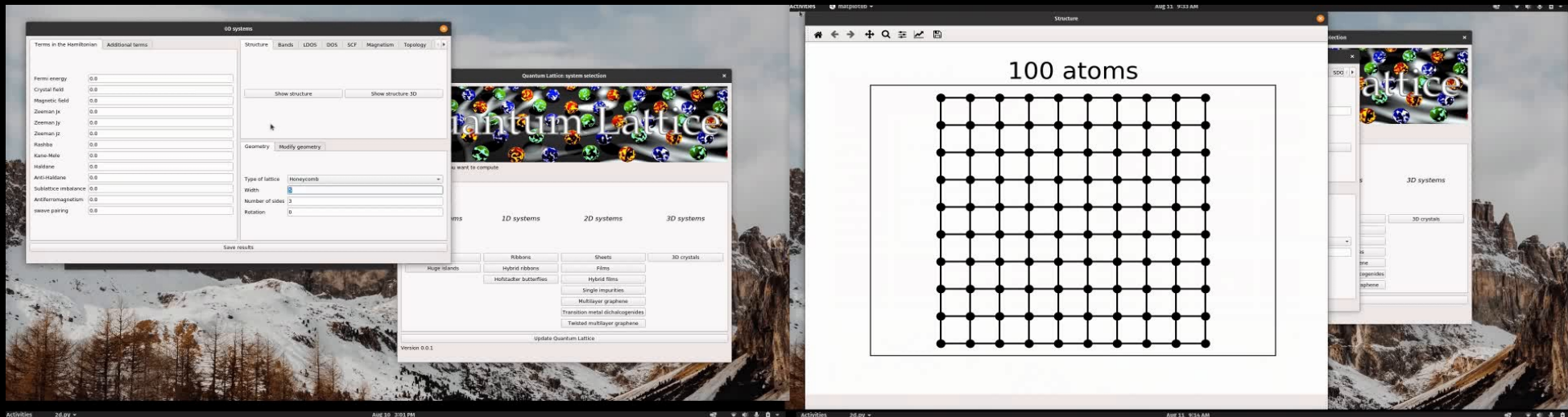
The YSR state wavefunction and the moire give rise to interference effects

Computing electronic properties

Quantum Lattice: A user interface to compute electronic properties



Quantum Lattice: open source interactive interface for tight binding modeling
<https://github.com/joselado/quantum-lattice>



Structure

Hamiltonian

Interlayer

Electric bias

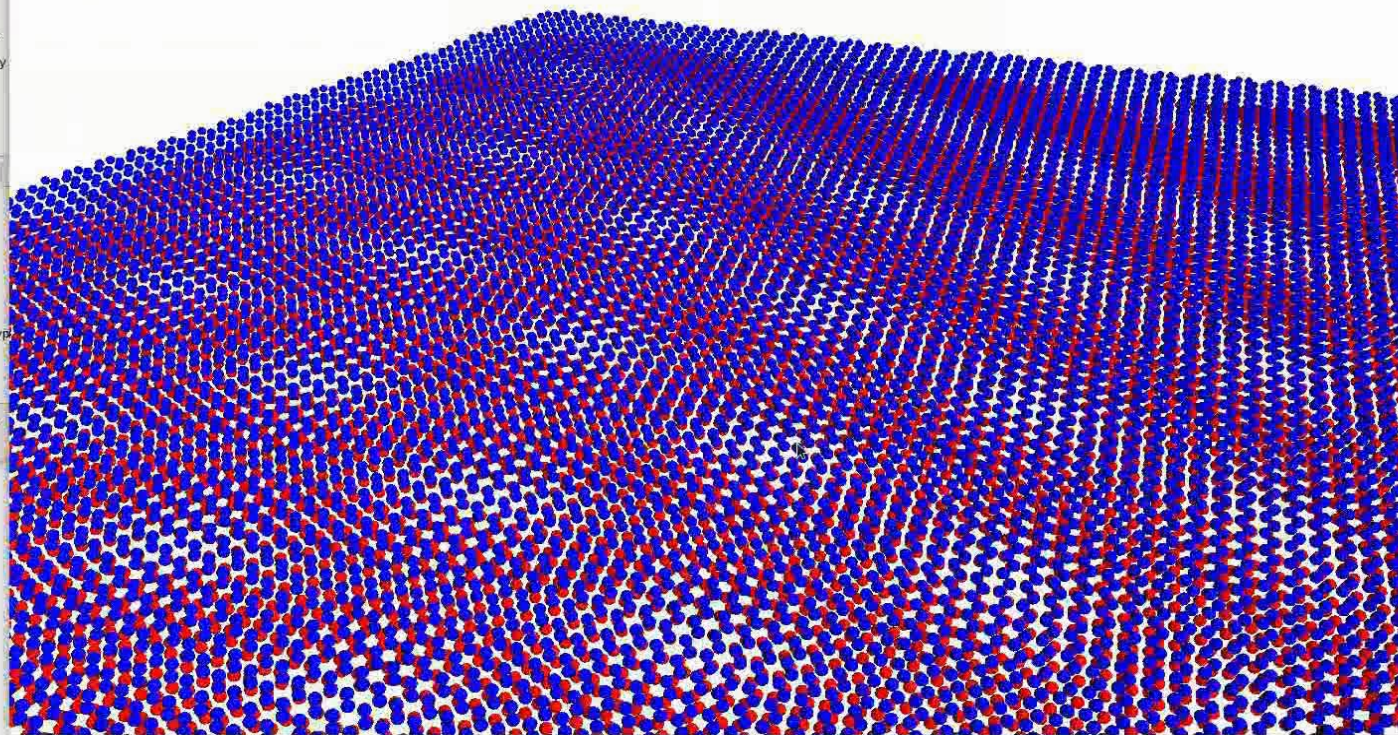
Fermi energy

Geometry

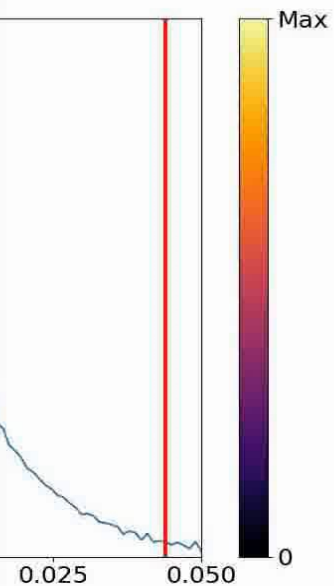
Cell size

Multilayer type

Parallelization



IPR

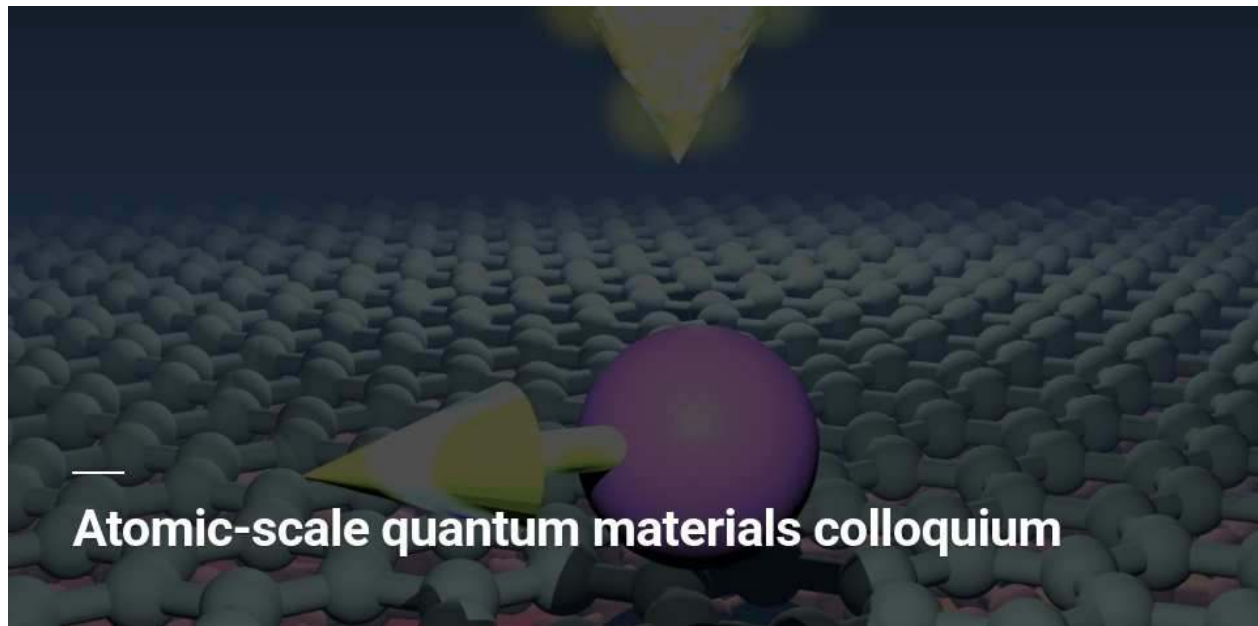


zoom rect, x=0.055054

Atomic-scale quantum materials colloquium

Colloquium series on atomic-scale manipulation and engineering of quantum materials

<https://asqm-colloquium.aalto.fi/>



Recordings of past talks available in the colloquium webpage



Leo Gross

IBM Research, Switzerland
Selective reactions between constitutional isomers by tip-induced chemistry
February 14th, 17:00 CET
[Video recording](#)



Abhay Pasupathy

Columbia University, US
Quantum phenomena at 2D interfaces
February 28th, 15:00 CET
[Video recording](#)



Ilija Zeljkovic

Rutgers College, US
Resonant imaging of elementary boson electronic phases in layered metals, 6/2/2020
March 18th, 17:00 CET
[Video recording](#)



Jennifer Hoffman

Harvard University, US
Studying quantum materials with acoustic metamaterials
March 26th, 17:00 CEST
Recording available from the organizers



Pavel Jelinek

Institute of Physics, Czech Academy of Sciences, Czech Republic
1D molecular chains with "exotic" quantum properties
April 11th, 16:00 CEST
[Video recording](#)



Raquel Queiroz

Columbia University, US
Imaginary ring states in topological materials
April 29th, 17:00 CEST
Recording available from the organizers



Philip Willke

Karlsruhe Institute of Technology, Germany
Single spin resonance of individual atoms and molecules on a surface
May 6th, 15:00 CEST
[Video recording](#)



Roser Valenti

Goethe-Universität Frankfurt, Germany
Strategies to design quantum materials with exotic properties
May 28th, 16:00 CEST
[Video recording](#)

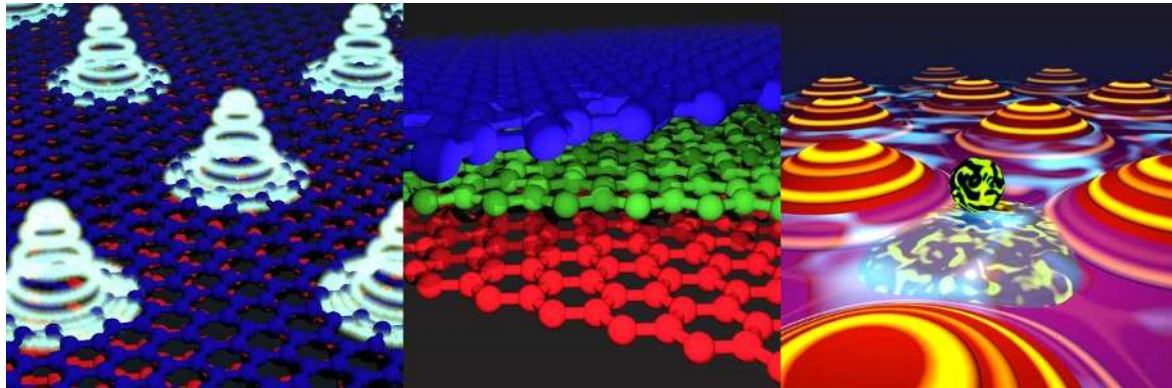


Shawulienu Kezilebieke

University of Jyväskylä, Finland
Designer quantum matter in van der Waals heterostructures
June 7th, 16:00 CEST

Take home

Impurities in twisted moire systems can have strong impacts in the low energy dispersion, substantially modifying topological and correlated states



Thank you!

Funding from

Phys. Rev. B 99, 245118 (2019)
Phys. Rev. Materials 3, 084003 (2019)
Phys. Rev. Research 2, 033357 (2020)
arXiv:2202.11003 (2022)

